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Towards Inverse Uncertainty Quantification in Software Development

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Outline

- Introduction & Background
 - Uncertainty
 - Bayesian reasoning
- Envisioned Approach
 - IUQ by combining Online MBT & Bayesian reasoning
- Current stage of the work
- Conclusion

Introduction

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- **Uncertainty**
 - imperfect and/or unknown information
 - $S?, E? \models R$ @ Designtime
 - sources of uncertainty (epistemic or aleatory) can be introduced into the system by
 - the system itself: structural uncertainty, algorithmic uncertainty, etc.
 - the environment: parameter uncertainty, usage profiles, network latency, etc.

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- **Objective**

- Inverse Uncertainty Quantification (IUQ) in software development
 - **discrepancy** between the measured data at runtime and the formal specification (i.e., a mathematical model)
 - **value calibration** of unknown parameters in the model

State of the art

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- **FUQ problem**

- [Epifani, C. et al., 2009] Model evolution by run-time parameter adaptation, in 2009 IEEE 31st International Conference on Software Engineering, May 2009, pp. 111–121
- [N. Esfahani et al., 2013] Uncertainty in Self-Adaptive Software Systems. Berlin, Heidelberg: Springer Berlin Heidelberg, 2013, pp. 214–238
- [Perez-Palacin et al., 2014] Uncertainties in the modeling of self-adaptive systems: A taxonomy and an example of availability evaluation, in Proceedings of the 5th ACM/SPEC Int. Conference on Performance Engineering, 2014, pp. 3–14
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- ...

- **Testing and Uncertainty**

- [A. S. Namin et al., 2010] Bayesian reasoning for software testing, in Proc. of the FSE/SDP Workshop on Future of Soft. Eng. Research, 2010, pp. 349–354
- [N. Walkinshaw et al., 2017] Uncertainty-driven black-box test data generation, in IEEE Int. Conf. on Software Testing, Verification and Validation, 2017
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Background

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- **Specification formalism**
 - Markov models s.t. the system state is fully observable and outcomes are partially under the control of a decision maker
 - CTMDPs \rightarrow CTMCs extension, nicely supported by powerful off-the-shelf model checking tools (e.g. MRMC - Markov Reward Model Checker)

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- **Bayesian inference**

- $y^m(\Theta) \simeq y^e$

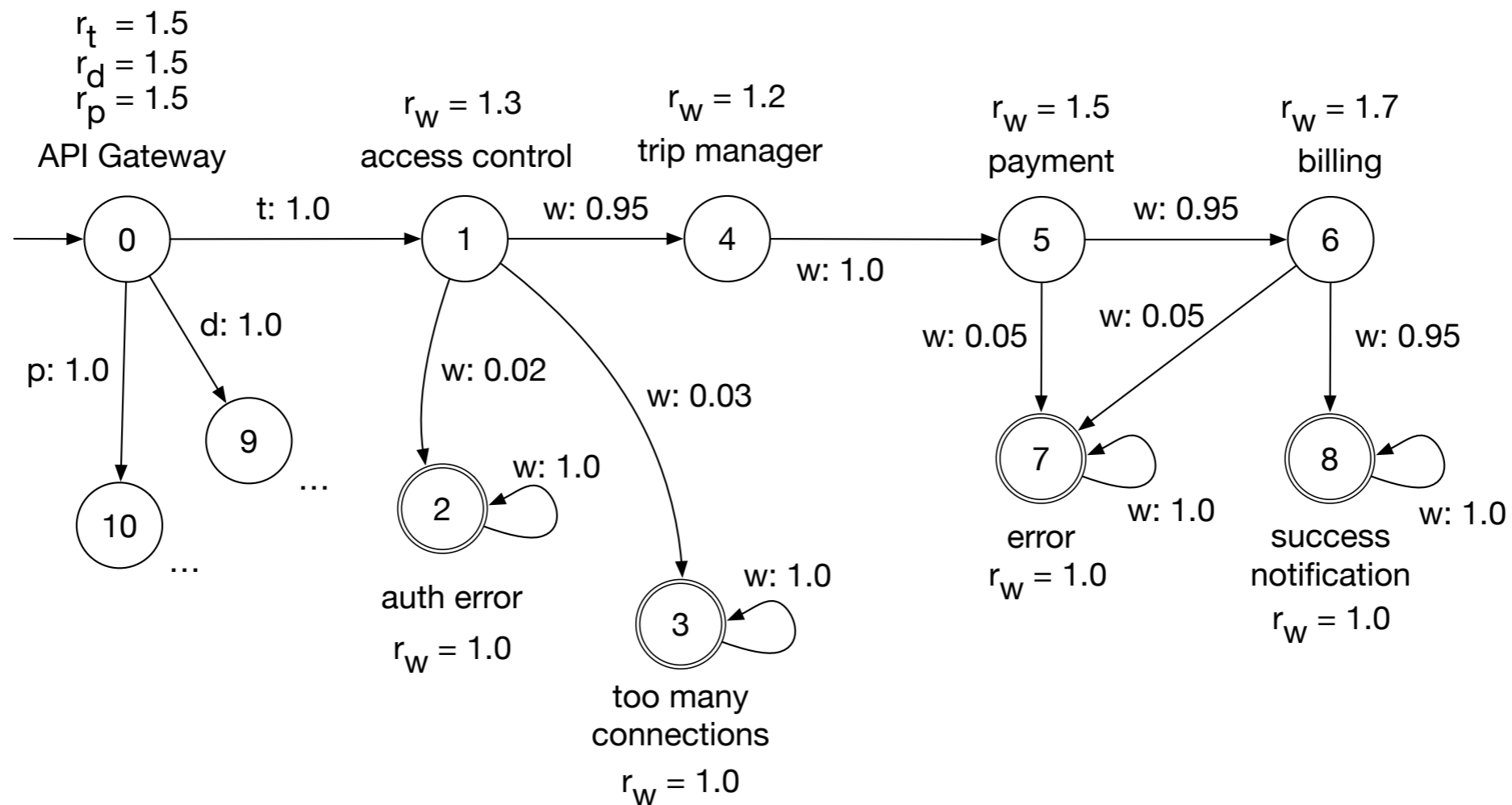
- methodology:

$$P(\Theta | y^e) \propto P(y^e | \Theta) \cdot P(\Theta)$$

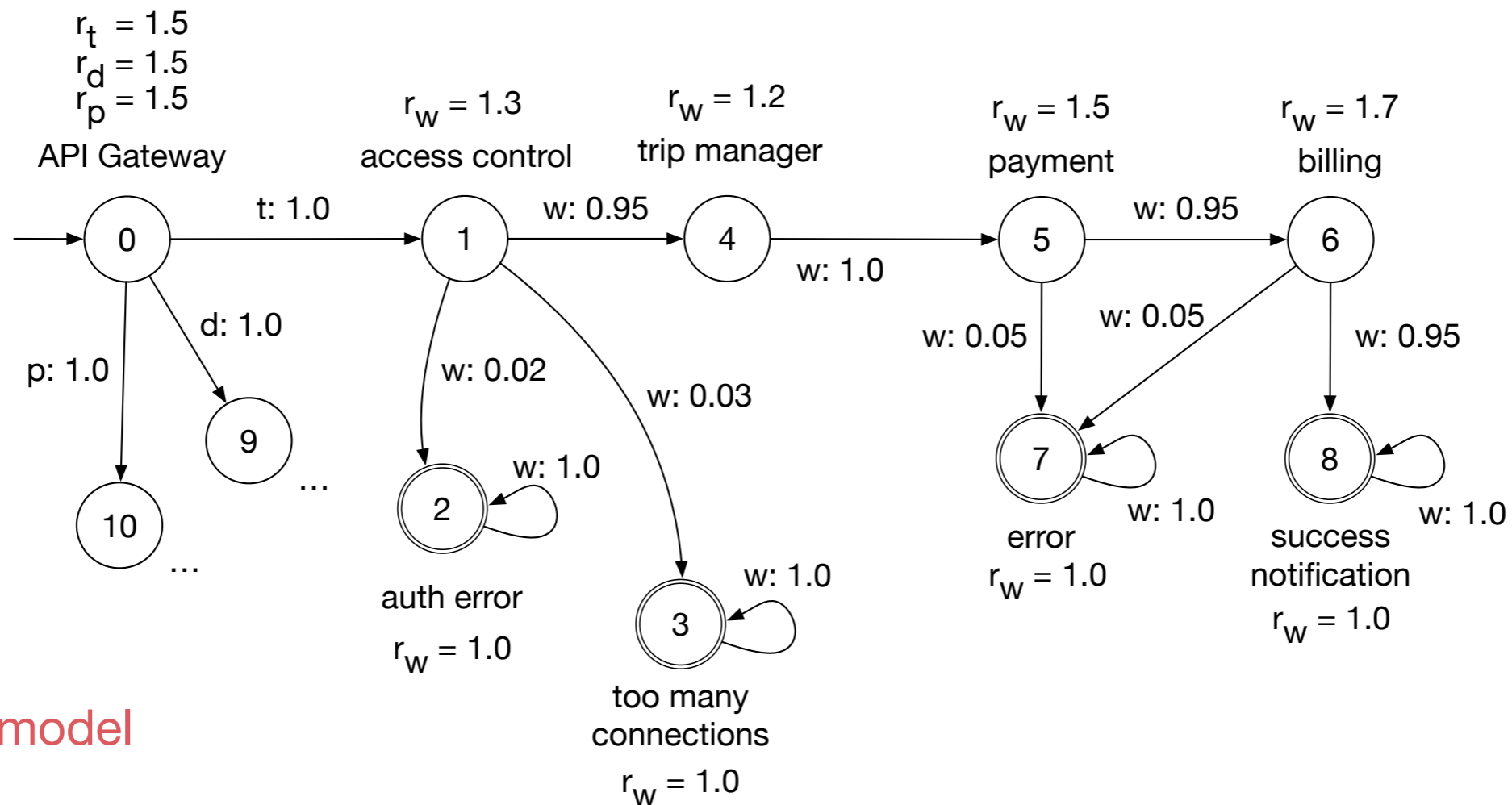
Prior probability

Posterior probability likelihood

A running example: the taxi-hailing application

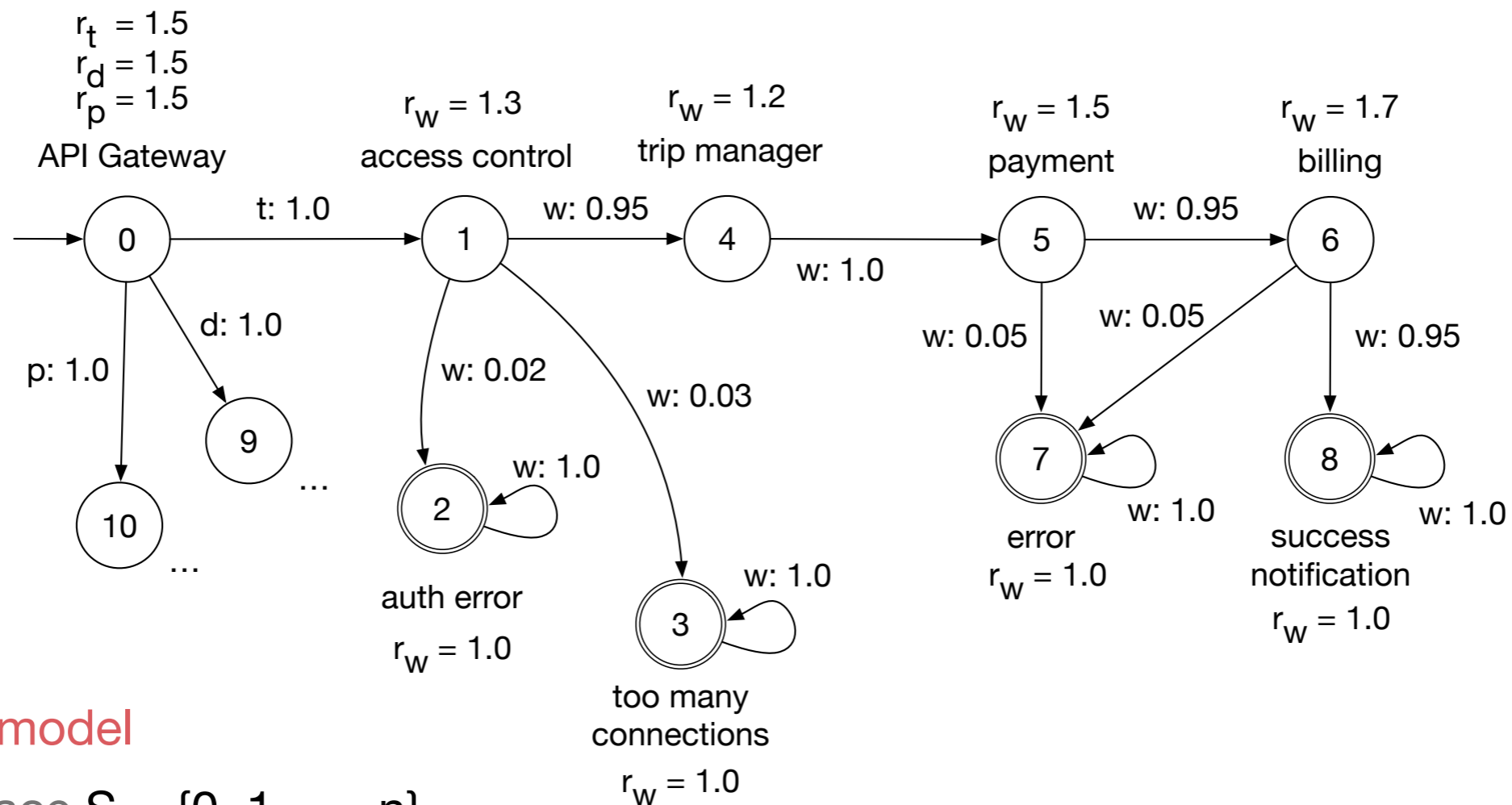


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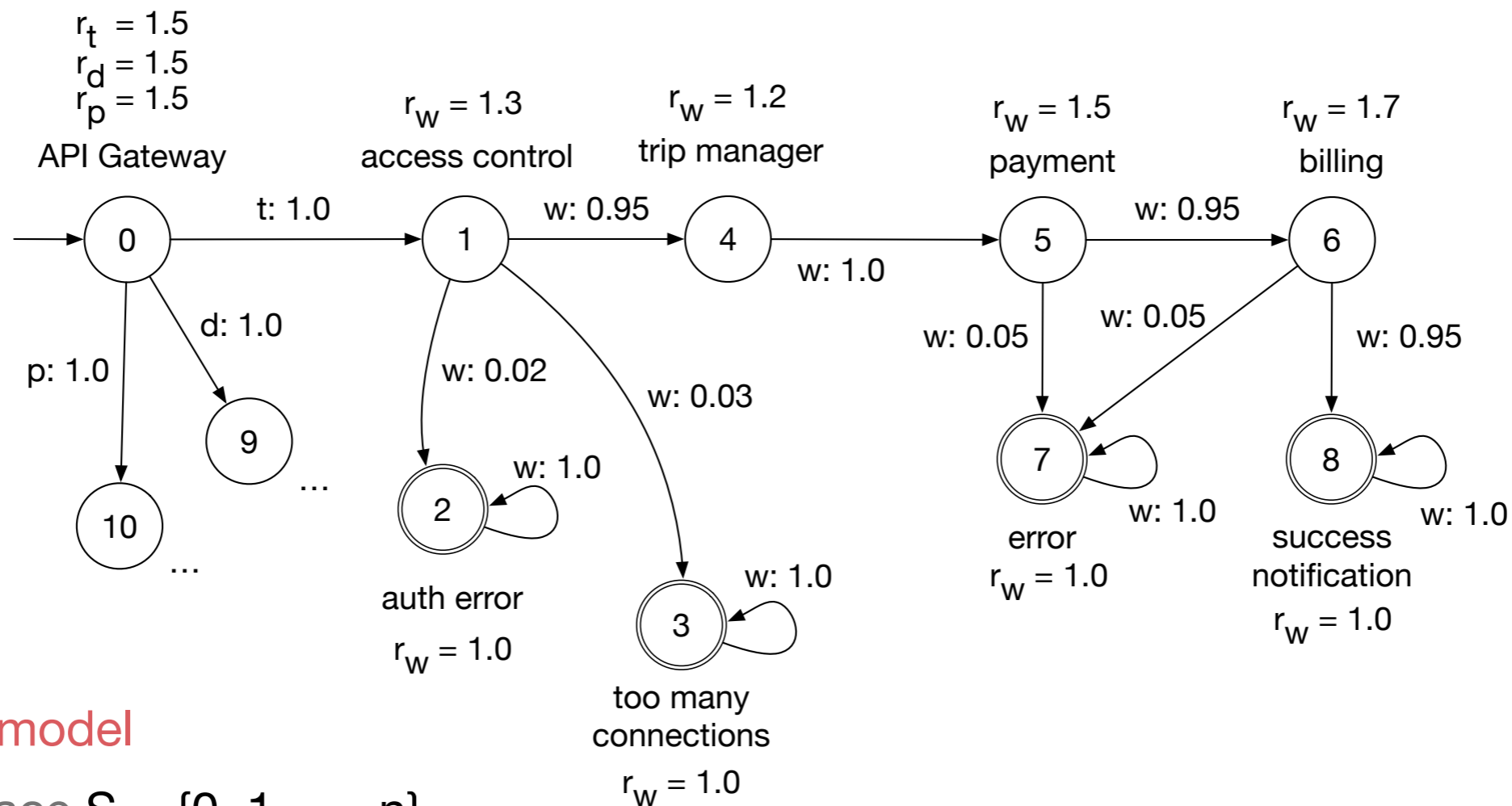
- CTMDP model

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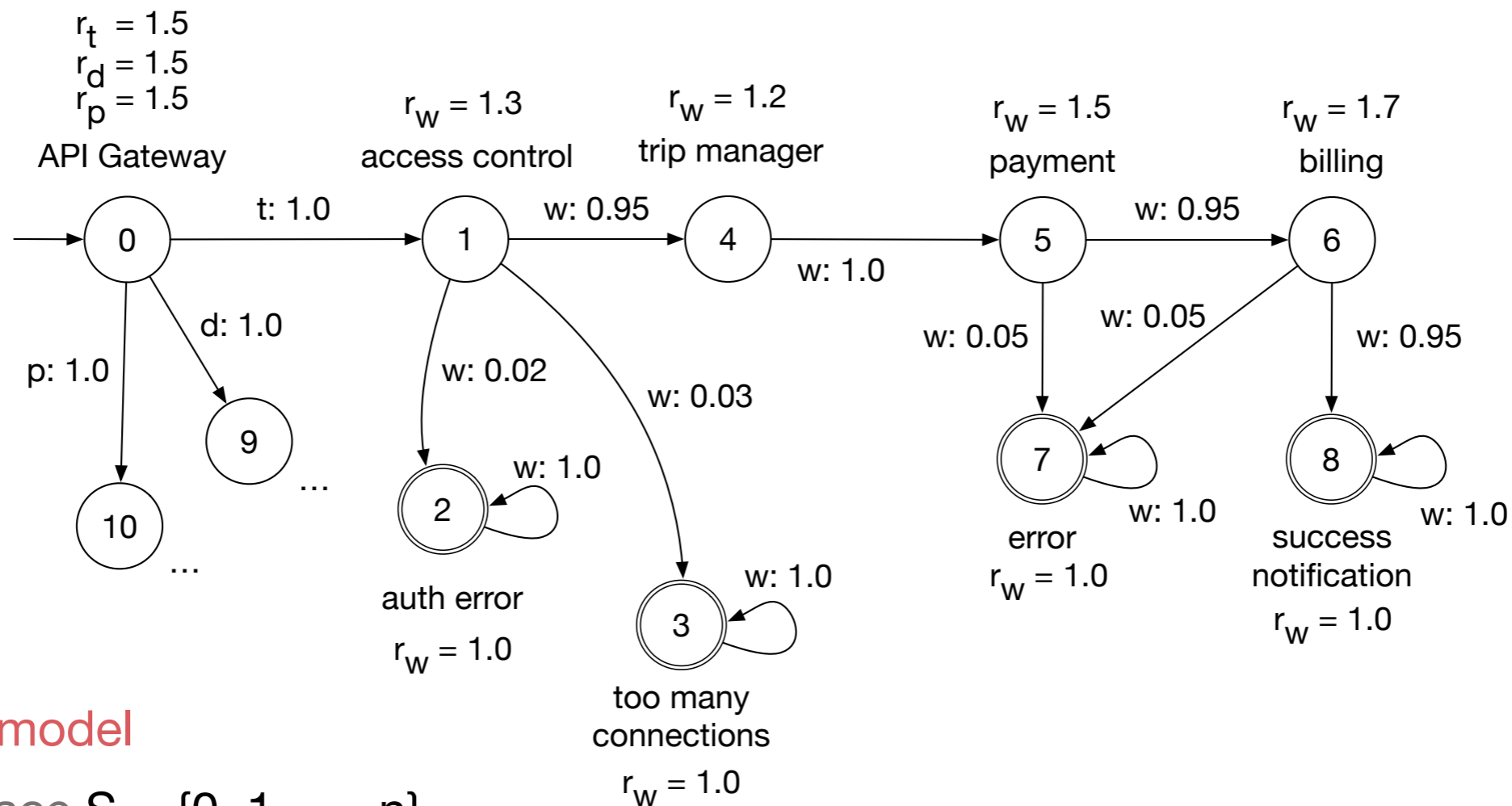
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- State space $S = \{0, 1, \dots, n\}$

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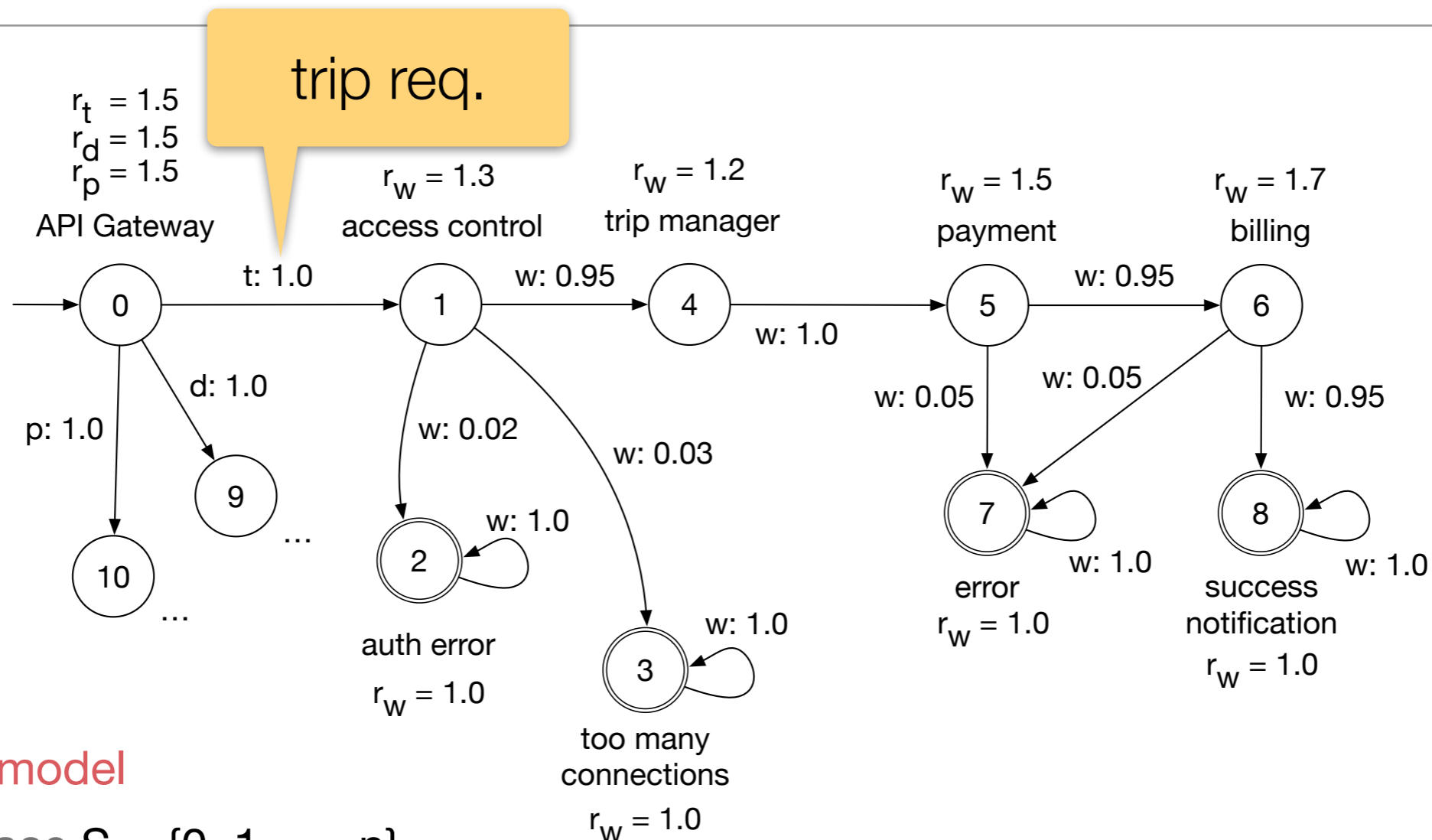
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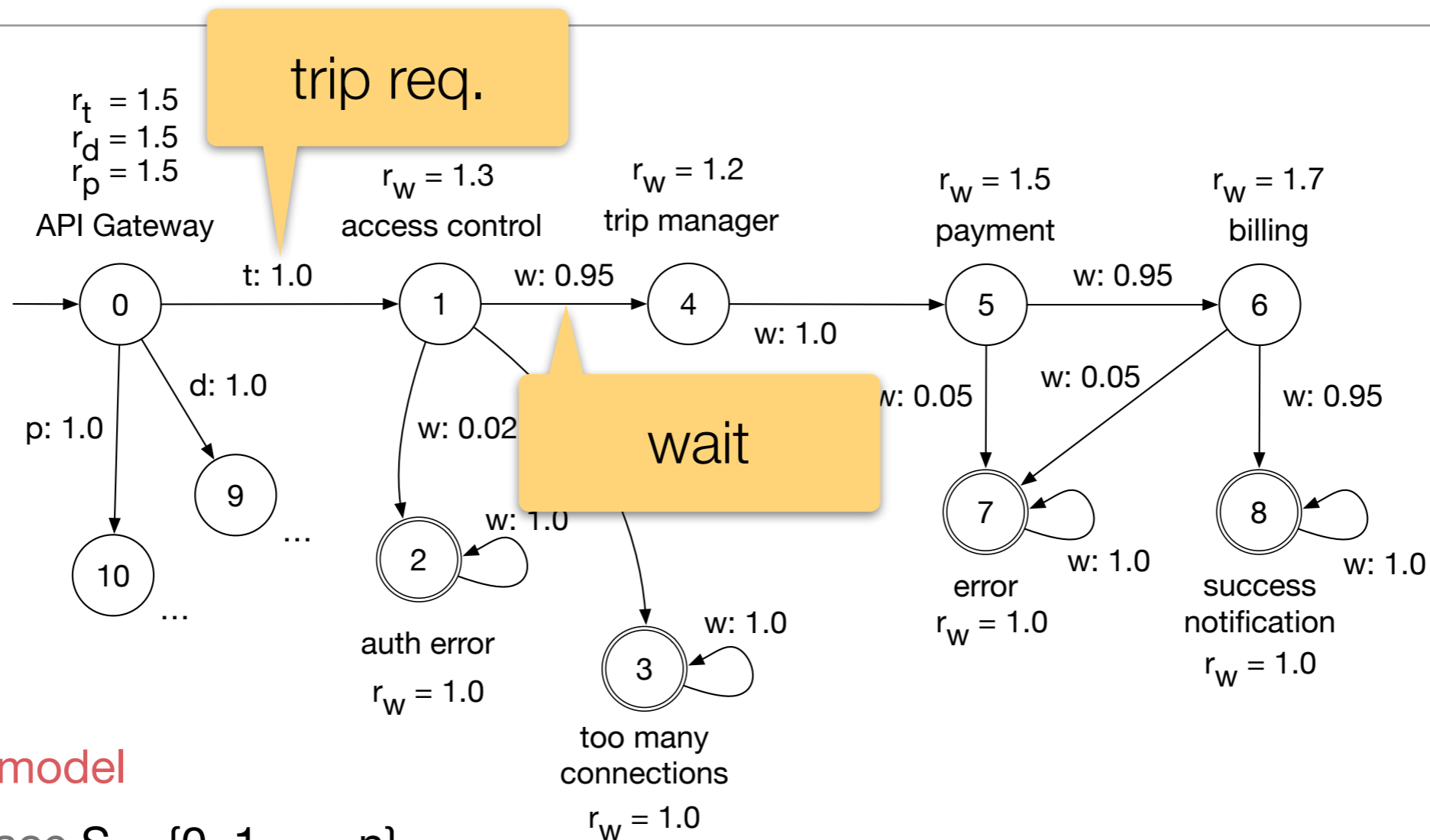
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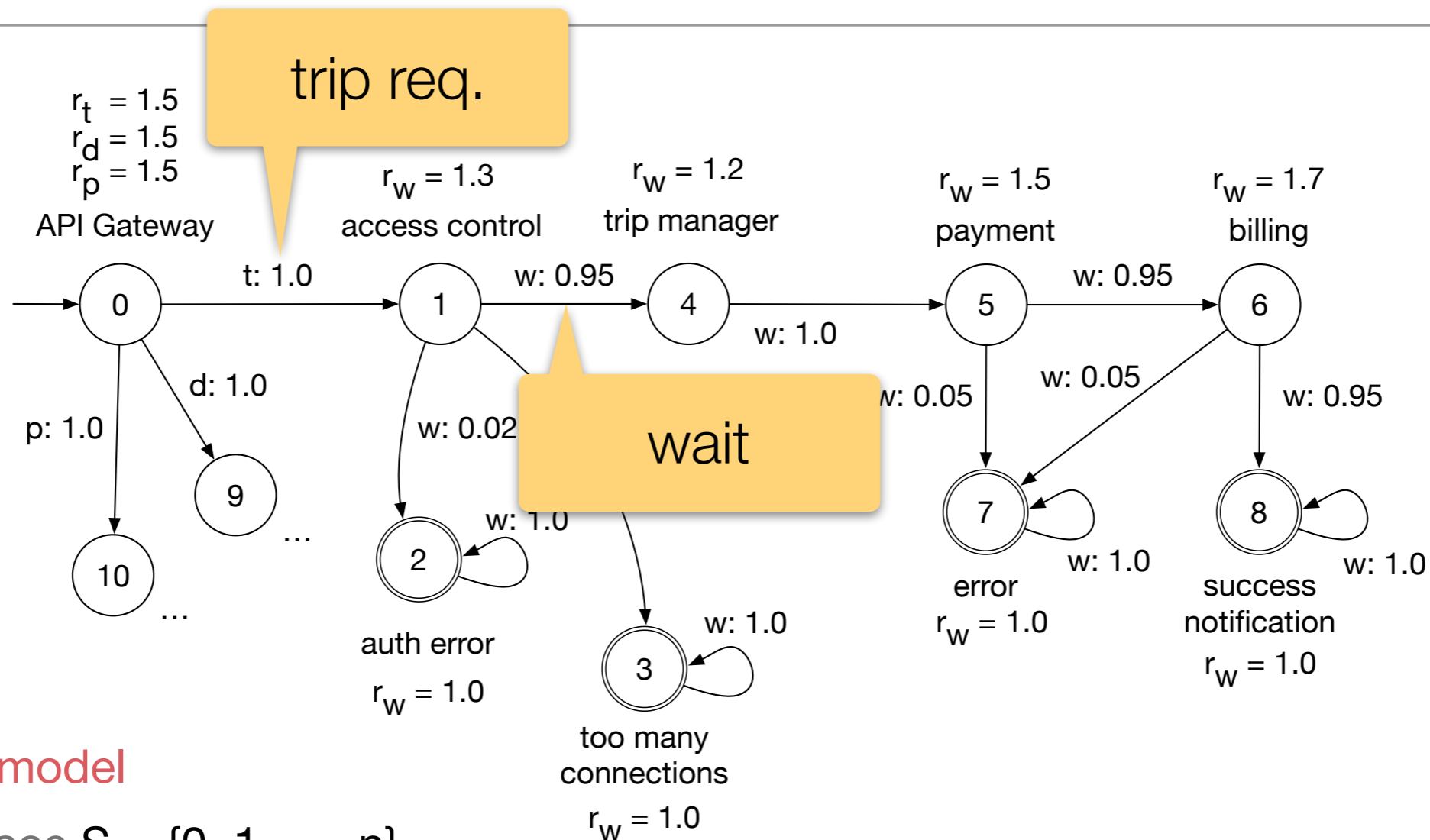
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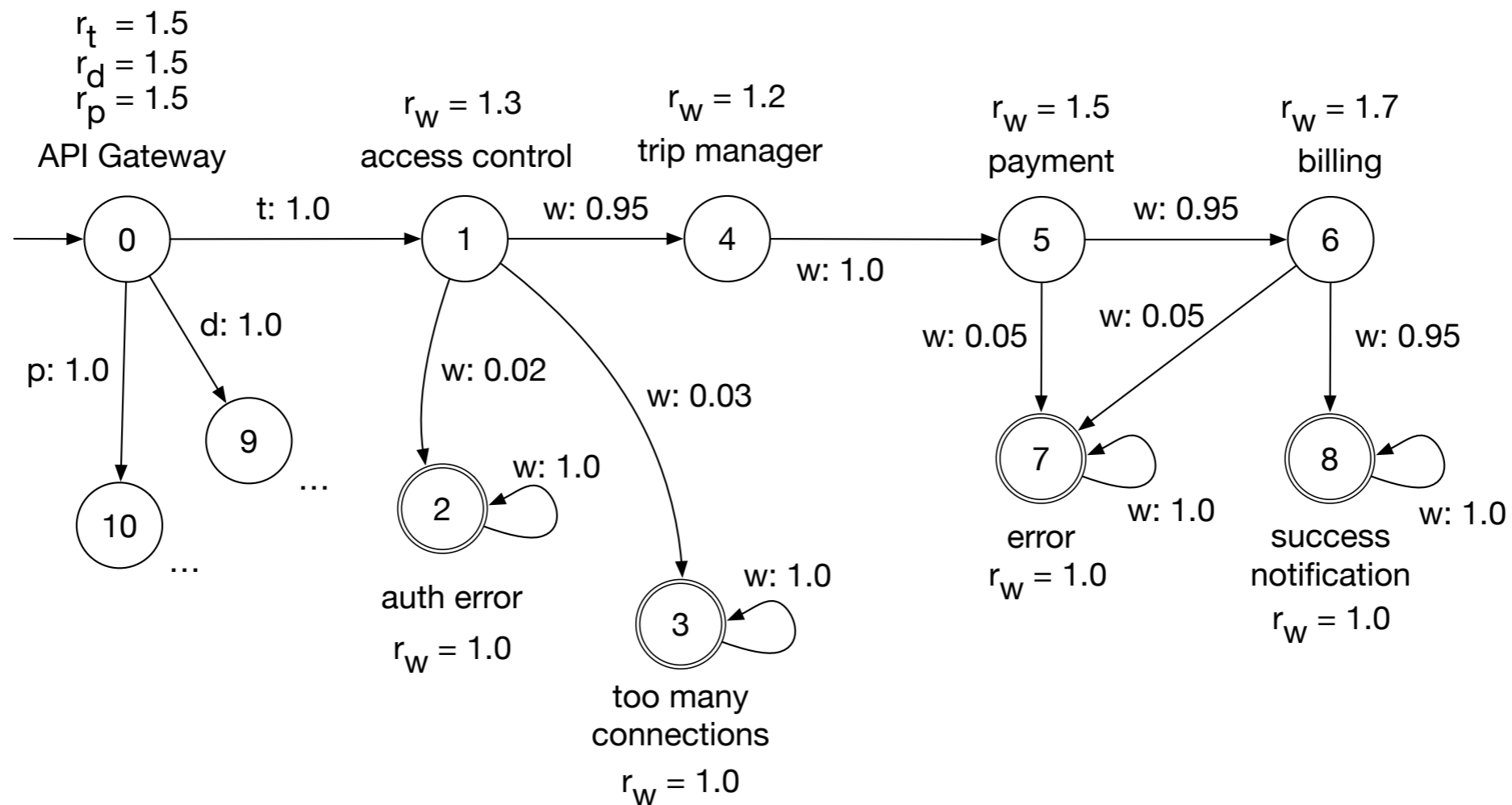
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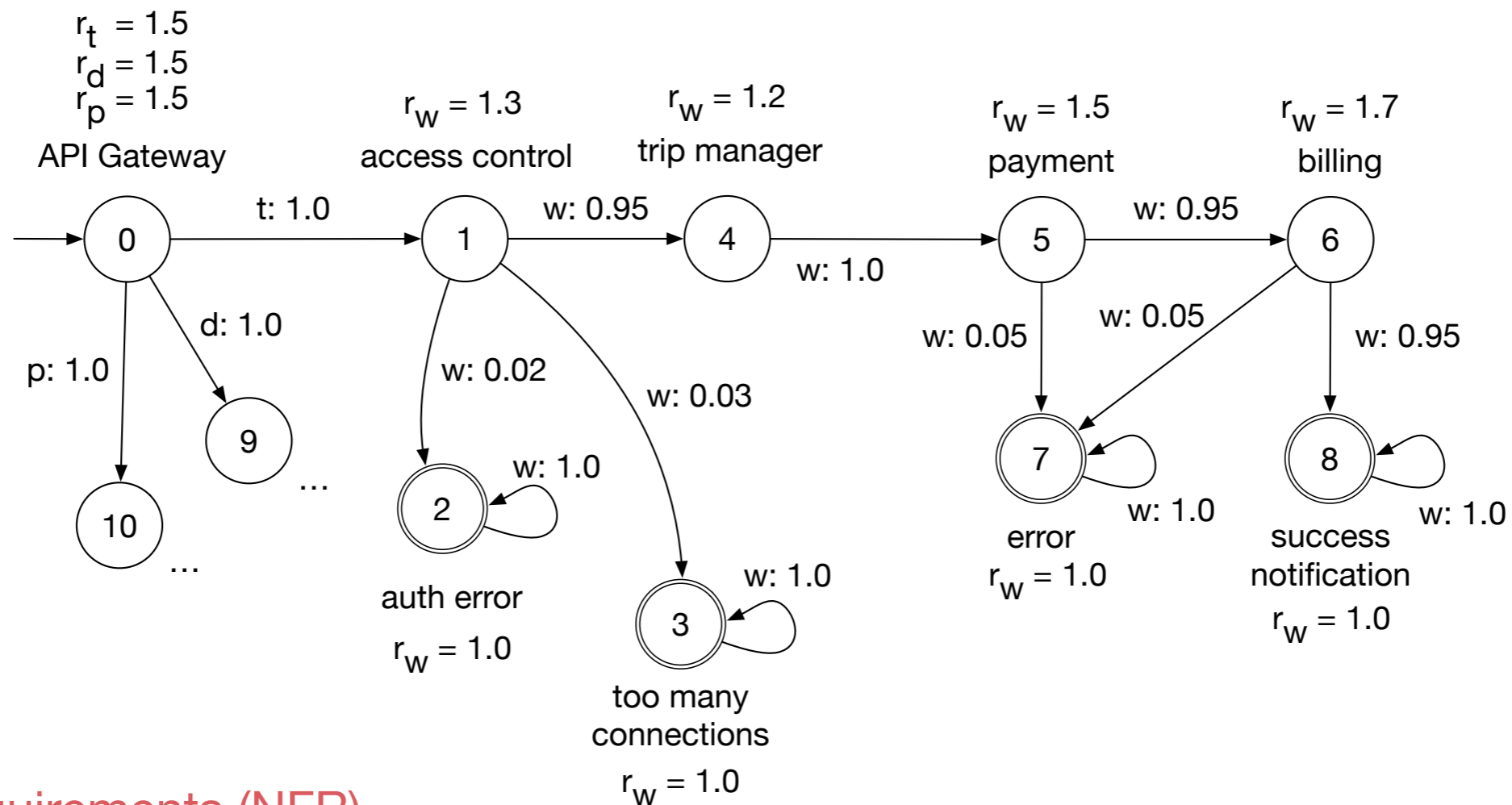


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- Transition probabilities $p_a(i, j) \in [0, 1]$
- Exponential sojourn time $r_a(i) \in \mathbb{R}_{>0}$; Rewards $R_a(i, j) = 0$, $\forall i \neq j$

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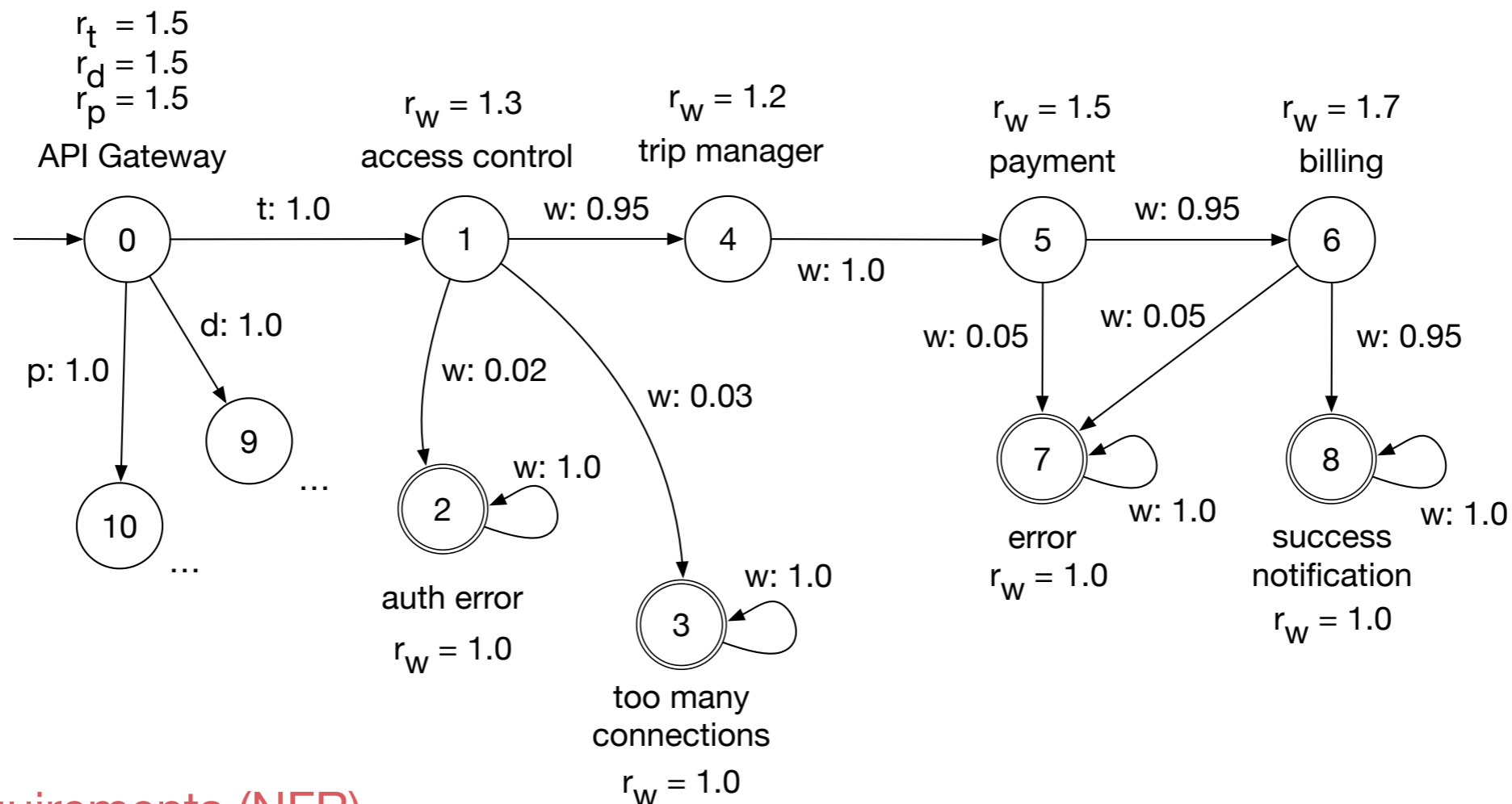


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- CSL Requirements (NFR)

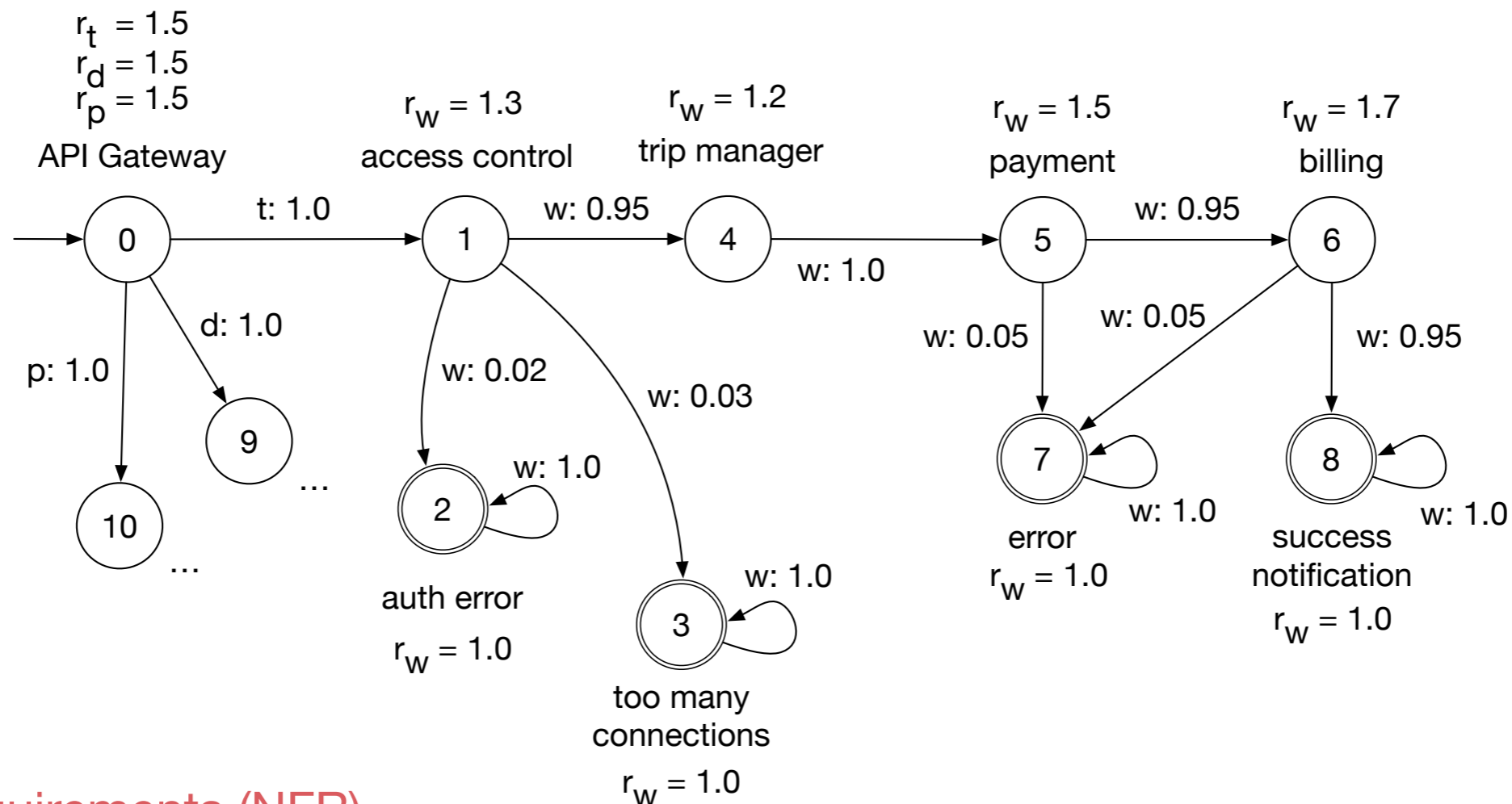
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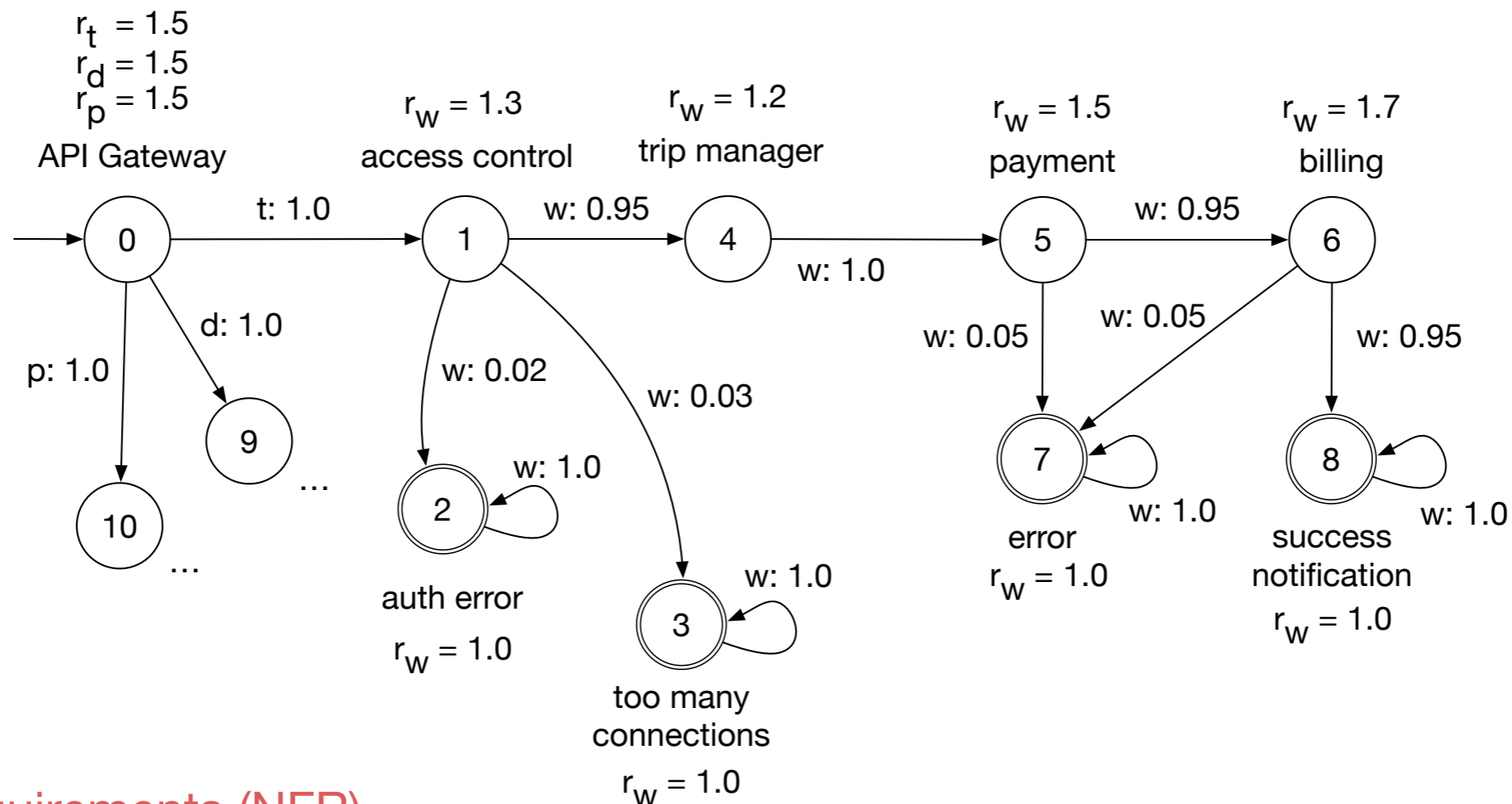
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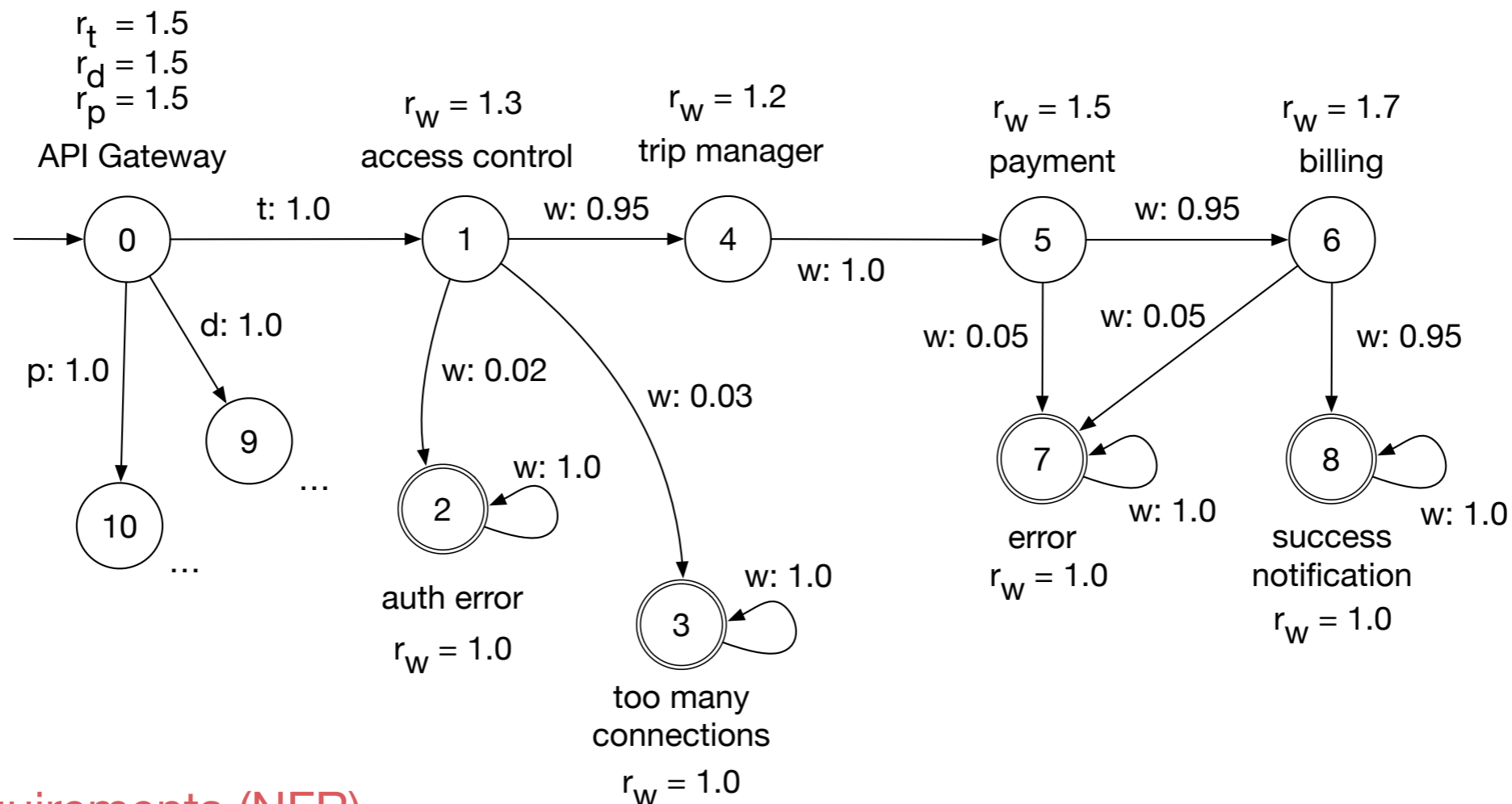
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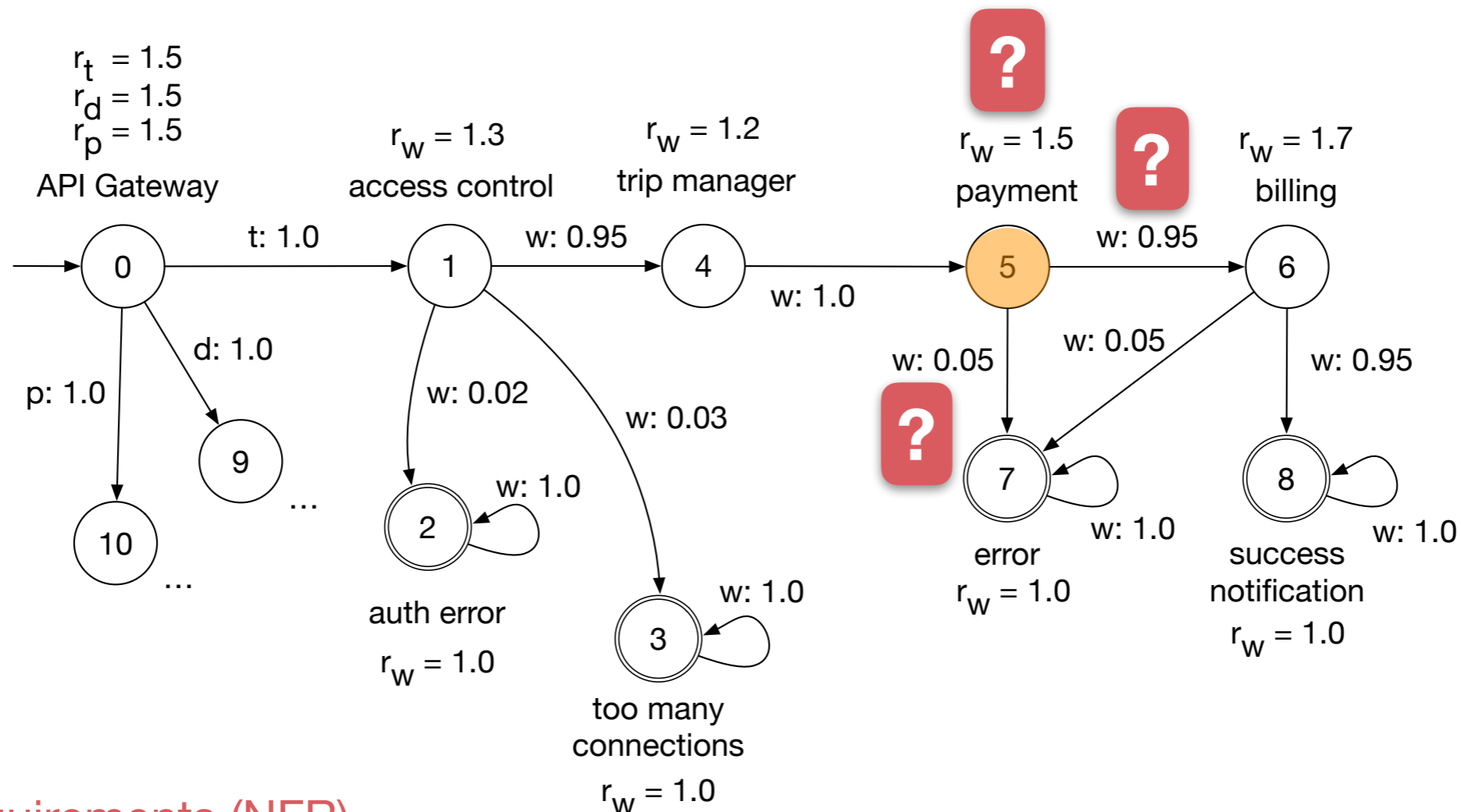


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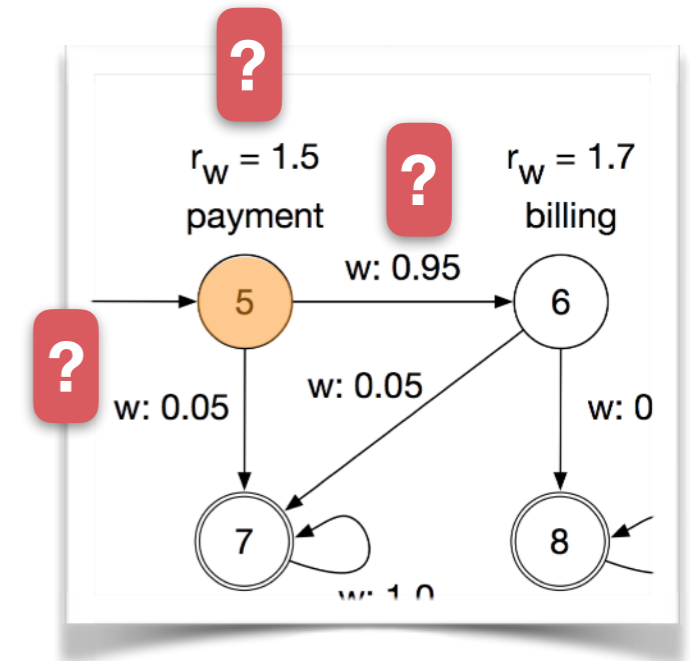


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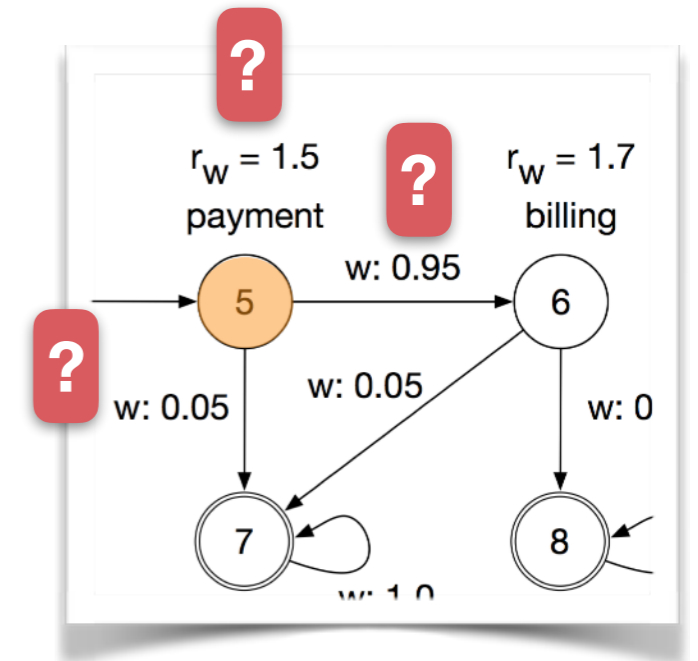
Inference using online MBT



Inference using online MBT

- Priors

- uncertain rates: $r_w(5) \sim \text{Ga}(a, b)$
- uncertain transition probabilities: $(p_w(5,6), p_w(5,7)) \sim \text{Dir}(\alpha_1, \alpha_2)$



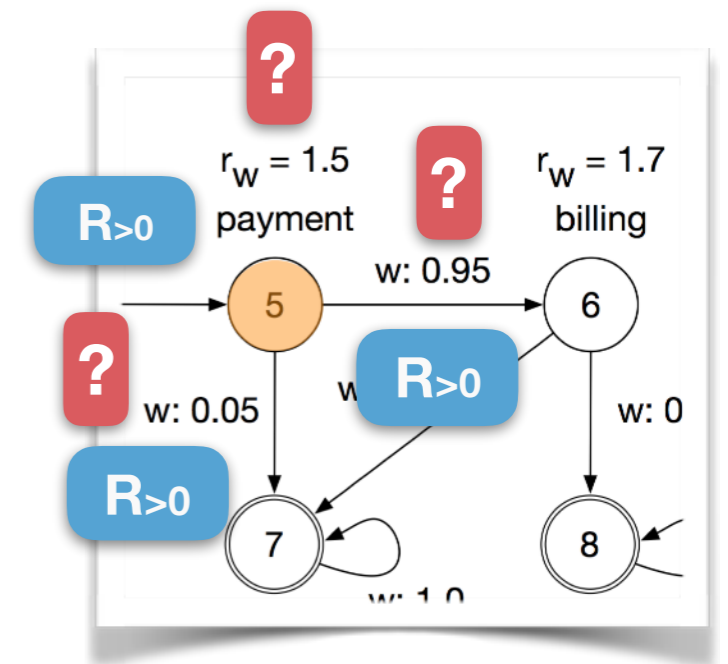
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- we set a reward $R_{>0}$ attached to uncertain components
- we compute a reward dependent policy π that maximizes some cumulative function on the rewards: $\sum_{i=0}^{\infty} \gamma^i R(s_i, s_{i+1})$



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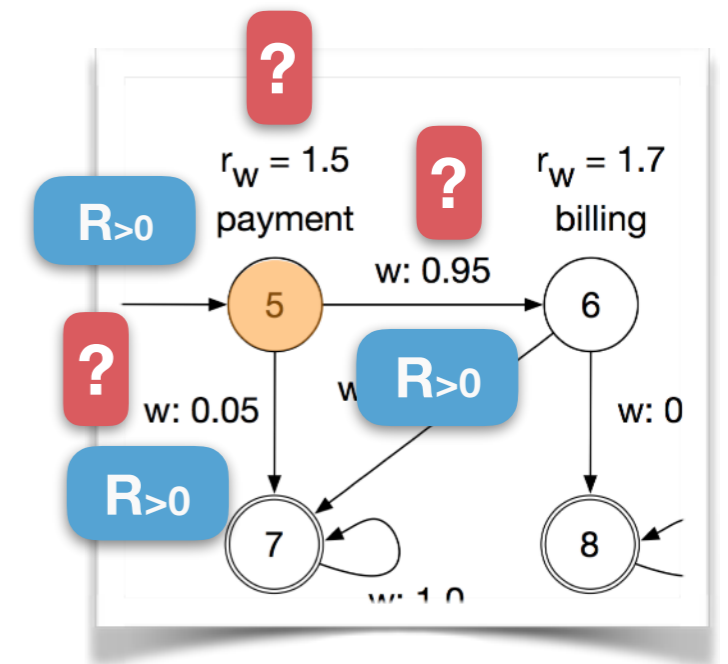
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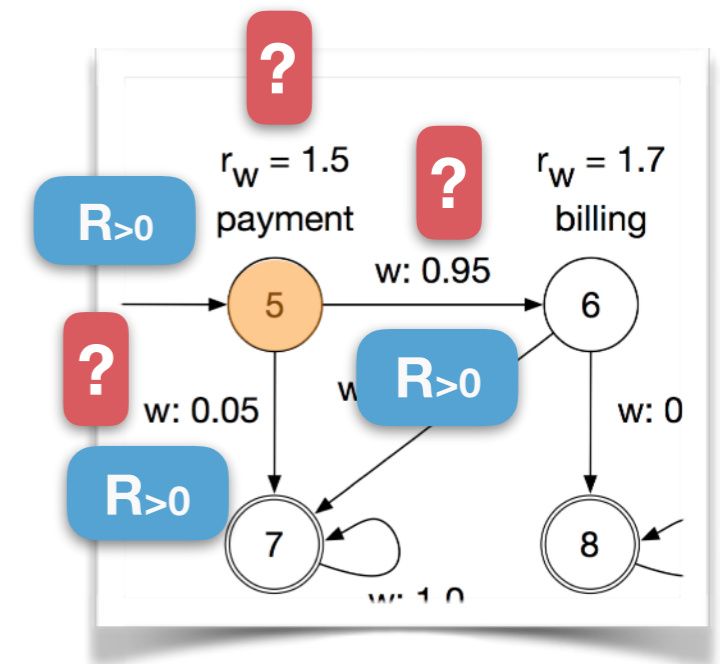
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- updating rules: $r_w(5) | y^e \sim \text{Ga}(a+n_5, b+T_5)$, $(p_w(5,6), p_w(5,7)) | y^e \sim \text{Dir}(\alpha_1+n_{5,6}, \alpha_2+n_{5,7})$
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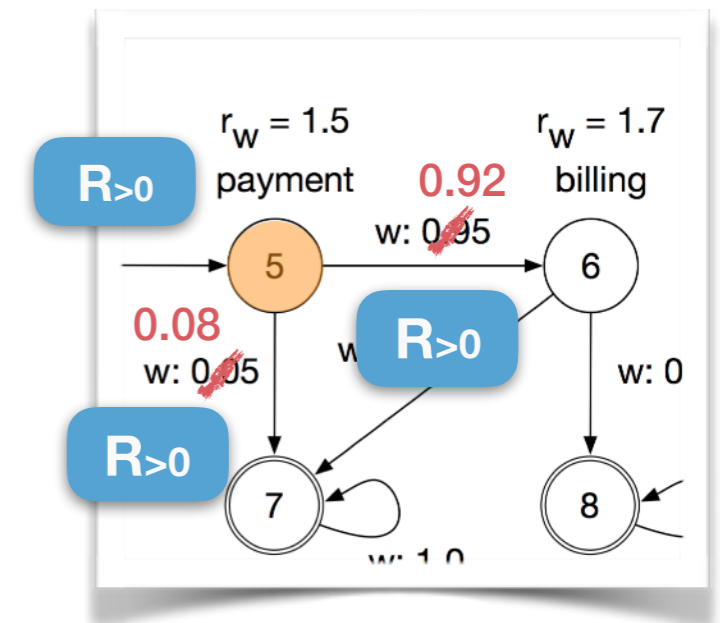
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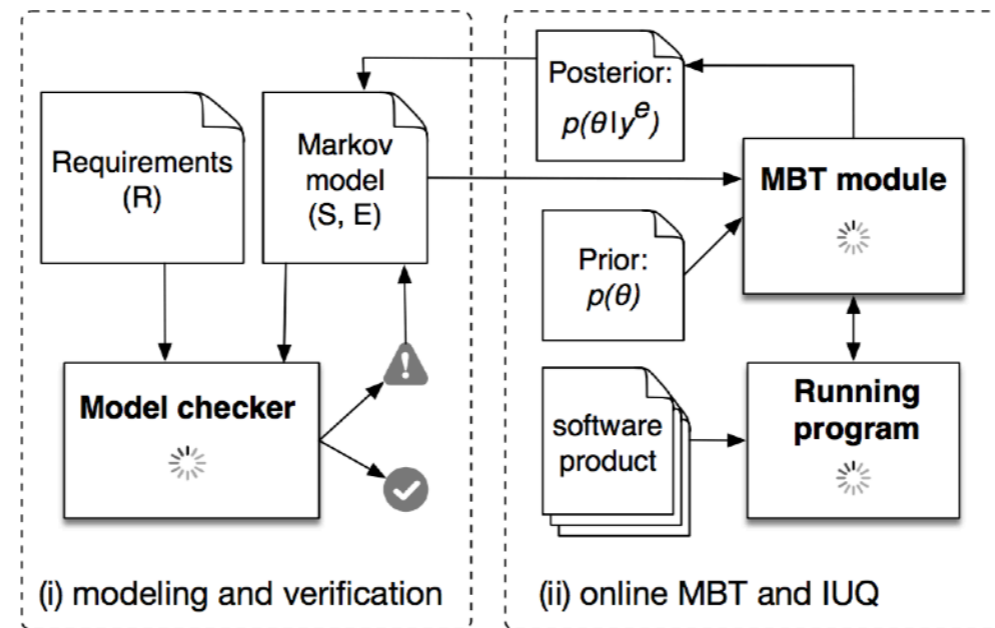
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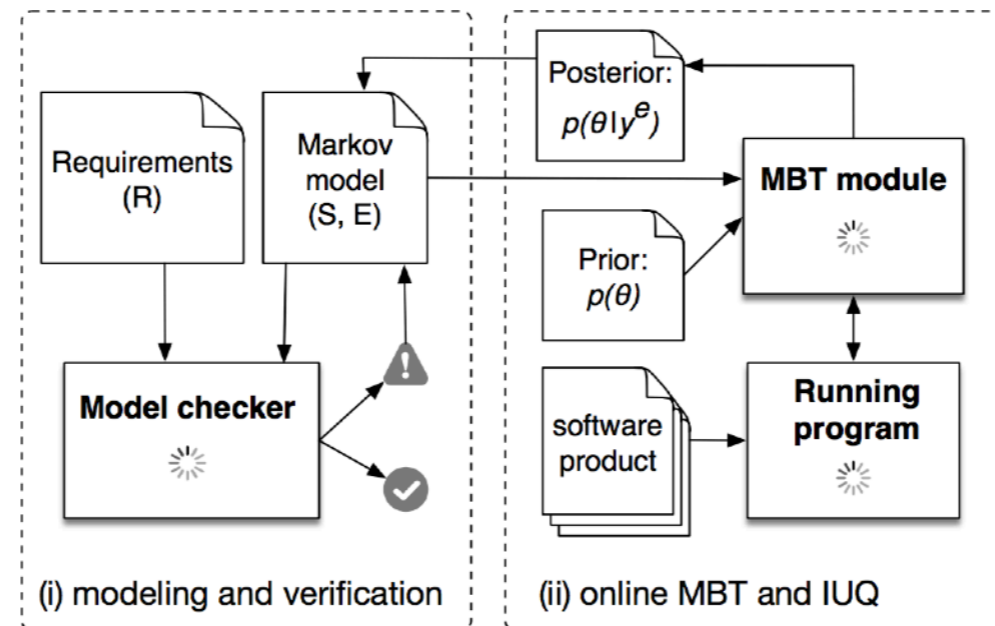


(NFR1) ~~X~~

Toolchain

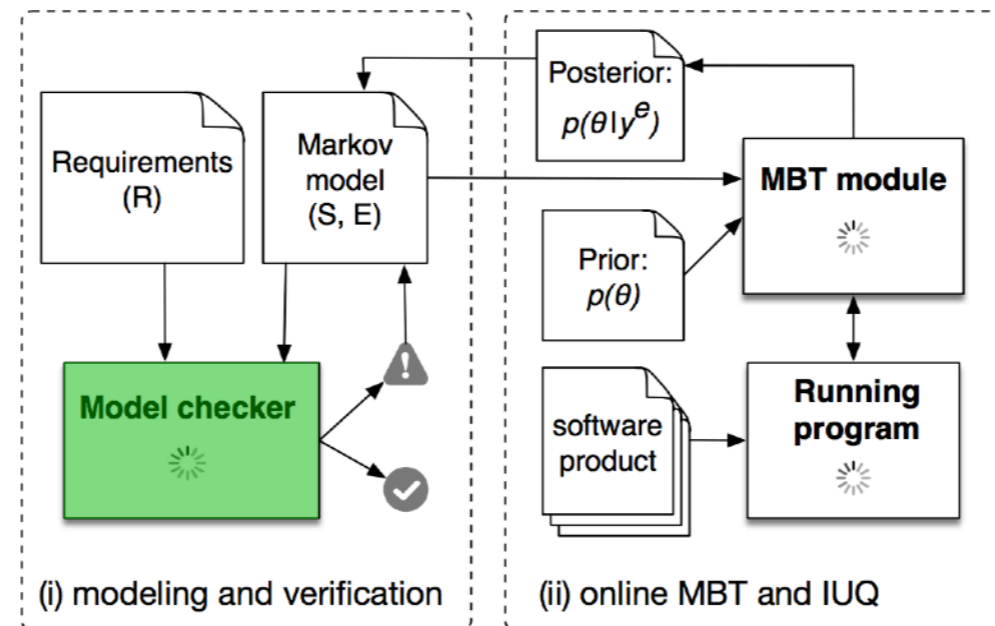


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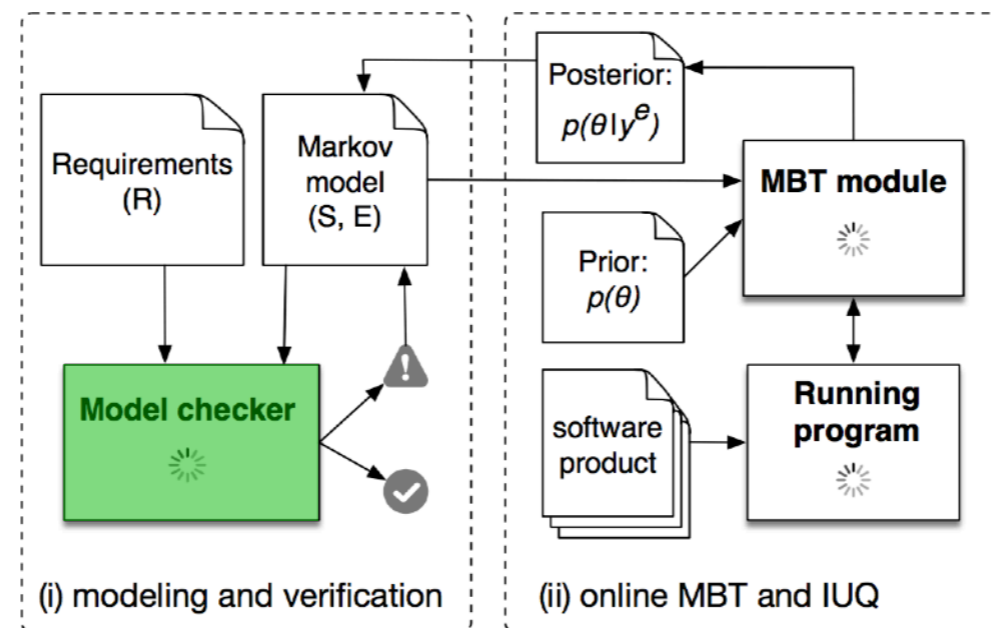
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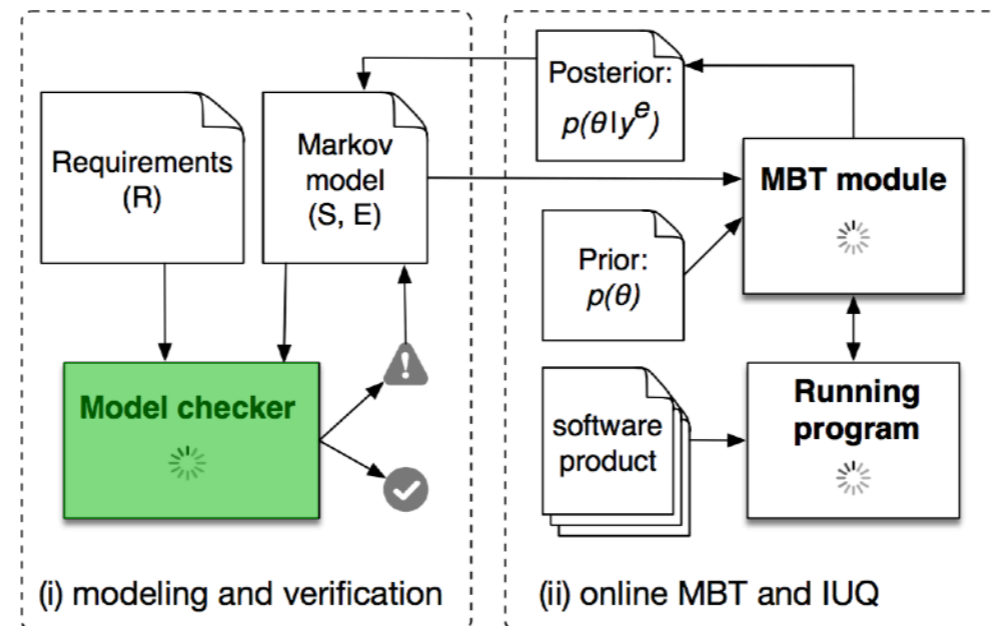
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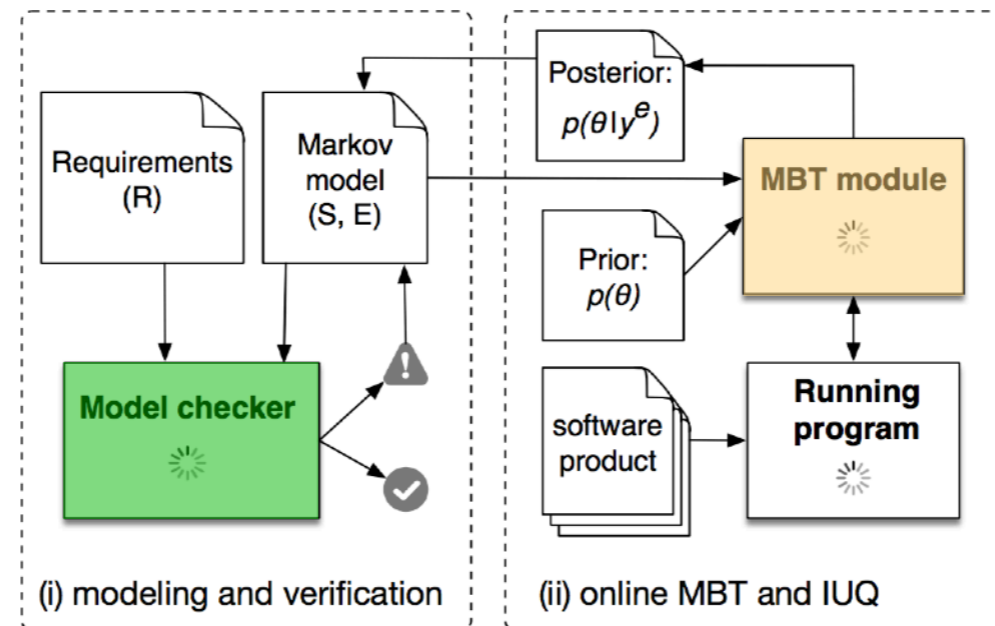
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 - a simple DSL aids the definition of the CTMDP model and automatically map actions to *observable/controllable* methods of the implementation (i.e., a Java program)
- **(ii) online MBT and IUQ**
 - we are in the process of validating the online MBT module with a realistic case-study deployed on a cloud infrastructure

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- systematic evaluation of the approach on realistic case studies
- allow to mix the uncertainty-based sampling method with user-defined strategies based on decrementing/fixed weights associated with controllable actions



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Thank you

Questions?

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