

On Approximate Diagnosability of Metric Systems

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Introduction

- Diagnosability corresponds to the possibility of detecting faults within finite delays
- Extensively investigated in the communities of discrete event systems, continuous control systems and also hybrid systems
- Current literature assume the exact knowledge of state of output variables except for

[Lunze, M&C-00] J. Lunze. Diagnosis of quantized systems based on a timed discrete–event model. IEEE Transactions on Man and Cybernetics – Part A: Systems and Humans, May 2000

[De Persis, CDC-13] C. De Persis. Detecting faults from encoded information. IEEE Conference on Decision and Control, 2013

This is **limiting** in concrete applications where sensors introduce errors in the state/output measurements

Introduction

Related literature

[Lunze, M&C-00] J. Lunze. Diagnosis of quantized systems based on a timed discrete–event model. IEEE Transactions on Man and Cybernetics – Part A: Systems and Humans, May 2000

[De Persis, CDC-13] C. De Persis. Detecting faults from encoded information. IEEE Conference on Decision and Control, 2013

Main issues

- [Lunze, M&C-00] and [De Persis, CDC-13] investigate diagnosability for quantized systems and model faults as additional inputs to the system
- [De Persis, CDC-13] considers discrete–time linear systems where faults are detected provided that they belong to an appropriate class of functions
- [Lunze, M&C-00] considers continuous–time nonlinear systems and detection is achieved in a stochastic setting

Introduction

Here:

- General class of **metric systems** able to model both discrete and continuous dynamics arising in complex heterogeneous systems as for example CPSoS
- Novel notion of **approximate diagnosability** that considers explicitly measurements corrupted by errors always introduced by non-ideal sensors in a real environment
- Relations between approximate diagnosability of metric systems that are in **approximate simulation**
- Application to approximate diagnosability of **nonlinear control systems** (with an infinite number of states and of inputs)

Outline

- Metric Systems
- Approximate diagnosability
- Main result
- Application to nonlinear control systems
- Example
- References and conclusions

Outline

- **Metric Systems**
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Systems

[Tabuada, Springer-09]

Definition

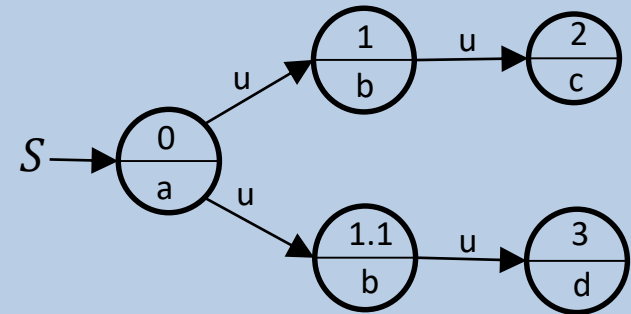
A system is a tuple

$$S = (X, X_0, U, \longrightarrow, Y, H)$$

where:

- X is the set of states
- $X_0 \subseteq X$ is the set of initial states
- U is the set of inputs
- $\longrightarrow \subseteq X \times U \times X$ is the transition relation
- Y is the set of outputs
- $H: X \rightarrow Y$ is the output function

We denote $(x, u, x') \in \longrightarrow$ by $x \xrightarrow{u} x'$



Systems

[Tabuada, Springer-09]

Definition

Given a system

$$S = (X, X_0, U, \rightarrow, Y, H)$$

and a sequence of transitions of S

$$x(0) \xrightarrow{u(0)} x(1) \xrightarrow{u(1)} \dots \xrightarrow{u(l-1)} x(l)$$

with $x(0) \in X_0$

- The sequence

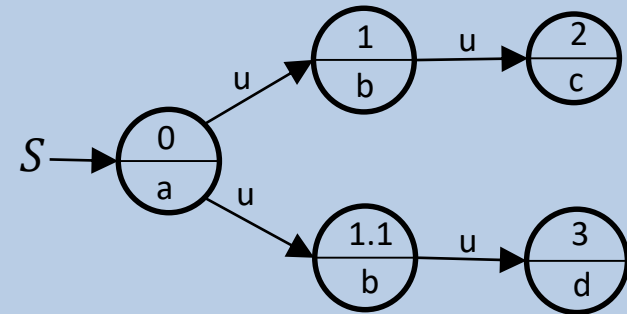
$$x(\cdot): x(0), x(1), \dots, x(l)$$

is called a state run of S

- The sequence

$$y(\cdot): H(x(0)), H(x(1)), \dots, H(x(l))$$

is called an output run of S



a state run:

$$x(\cdot): 0, 1, 2$$

corresponding output run:

$$y(\cdot): a, b, c$$

Systems

[Tabuada, Springer-09]

Classification:

A system $S = (X, X_0, U, \longrightarrow, Y, H)$ is

- countable if X and U are countable sets
- symbolic if X and U are finite sets
- deterministic if for any $x \in X$ and for any $u \in U$ there exists at most one transition

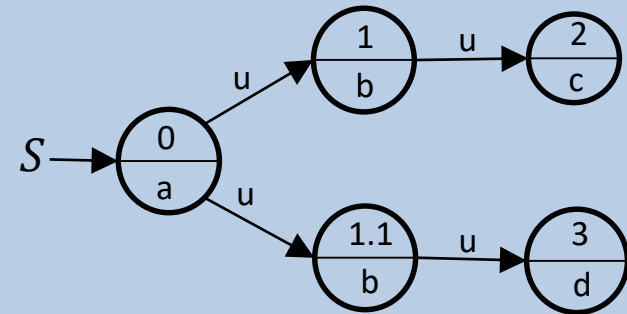
$$x \xrightarrow{u} x',$$

and nondeterministic, otherwise

- metric if X is equipped with a metric

Remark

Metric systems useful in modeling heterogenous dynamics arising in e.g. CPSoS



System S is:

- countable
- symbolic
- nondeterministic
- metric with metric

$$d(x_1, x_2) = \|x_1 - x_2\|$$

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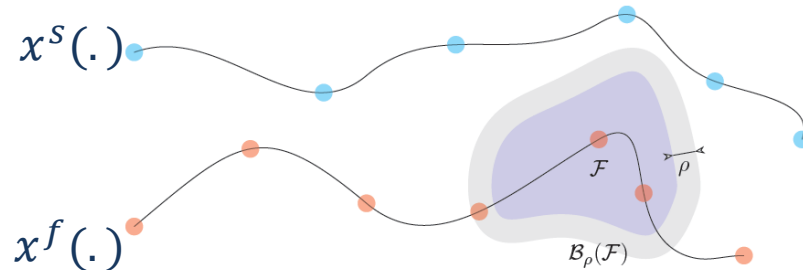
Approximate diagnosability

Given a metric system S , a set of faulty states $F \subseteq X$ and a desired accuracy $\rho \geq 0$

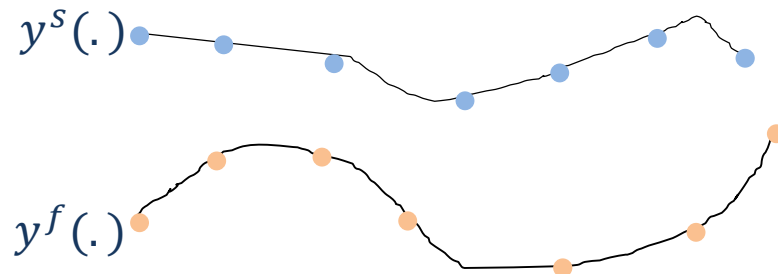
System S is (ρ, F) -diagnosable if

for any pair of state runs $x^f(\cdot)$ and $x^s(\cdot)$ of S such that

- $x^f(\cdot)$ reaches F in finite time
- $x^s(\cdot)$ does not reach $B_\rho(F)$ in finite time



the corresponding output runs are different within a finite delay Δ



Approximate diagnosability

Definition

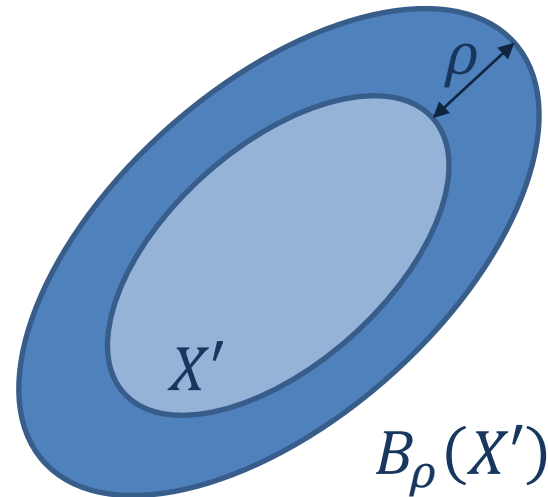
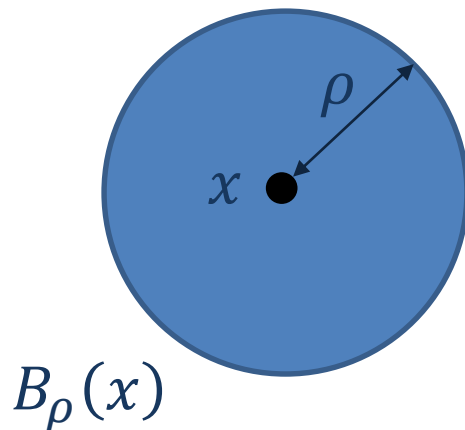
Consider a metric system

$$S = (X, X_0, U, \rightarrow, Y, H)$$

with metric \mathbf{d} , and denote for any $\rho \geq 0$, $x \in X$ and $X' \subseteq X$

$$B_\rho(x) = \{x' \in X \mid \mathbf{d}(x, x') \leq \rho\}$$

$$B_\rho(X') = \bigcup_{x' \in X'} B_\rho(x')$$



Approximate diagnosability

Definition

Consider a metric system

$$S = (X, X_0, U, \rightarrow, Y, H)$$

with metric \mathbf{d} , and denote for any $\rho \geq 0$, $x \in X$ and $X' \subseteq X$

$$B_\rho(x) = \{x' \in X \mid \mathbf{d}(x, x') \leq \rho\}$$

$$B_\rho(X') = \bigcup_{x' \in X'} B_\rho(x')$$

Consider a set $F \subseteq X$ of faulty states of S with $F \cap X_0 = \emptyset$.

Given a desired accuracy $\rho \geq 0$, system S is (ρ, F) -diagnosable if:

There exists a finite delay $\Delta \in \mathbb{N}$, such that for any pair of state runs $x^f(\cdot)$ and $x^s(\cdot)$ of S for which there exists $t \in \mathbb{N}$ such that

- $x^f(t) \in F$ and $x^f(t') \notin F$ for all $t' \in [0; t - 1]$
- $x^s(t'') \notin B_\rho(F)$ for all $t'' \in [0; t + \Delta]$

the corresponding output runs $y^f(\cdot)$ and $y^s(\cdot)$ are different at some $t' \in [0; t + \Delta]$

Approximate diagnosability

When $\rho = 0$ approximate diagnosability boils down to exact diagnosability as in [De Santis & Di Benedetto, Autom-2017], see also the overview [Zaytoon & Lafortune, ARC-13] and references therein.

Checking approximate diagnosability:

Proposition

For nonblocking metric symbolic systems S , the notion of approximate diagnosability can be checked with

- Space computational complexity $O(\text{card}(X)^2)$
- Time computational complexity $O(\text{card}(X)^5)$

Proof

Slight extension of algorithms proposed in [De Santis & Di Benedetto, Autom-2017] from exact diagnosability to approximate diagnosability. Details are reported in the paper

Outline

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Approximate simulation

[Girard & Pappas, TAC-07]

Definition

Consider $S_i = (X_i, X_{0,i}, U_i, \rightarrow_i, Y_i, H_i)$, $i = 1, 2$ with X_1 and X_2 subsets of some set X with metric d and let $\varepsilon \geq 0$ be a given accuracy. A relation

$$R \subseteq X_1 \times X_2$$

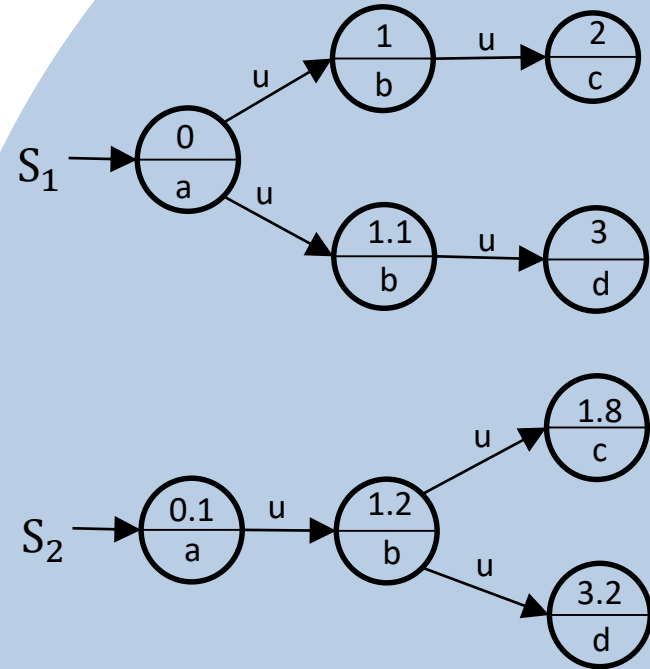
is an ε -approximate simulation relation from S_1 to S_2 if

1. $\forall x_1 \in X_{0,1} \exists x_2 \in X_{0,2}$ such that $(x_1, x_2) \in R$
2. $\forall (x_1, x_2) \in R, d(x_1, x_2) \leq \varepsilon$
3. $\forall (x_1, x_2) \in R, H_1(x_1) = H_2(x_2)$
4. $\forall (x_1, x_2) \in R$, if $x_1 \xrightarrow{u_1}_1 x'_1$ then $x_2 \xrightarrow{u_2}_2 x'_2$ such that $(x'_1, x'_2) \in R$

Metric system S_1 is ε -simulated by metric system S_2 , denoted

$$S_1 \preceq_{\varepsilon} S_2$$

if there exists an ε -approximate simulation relation from S_1 to S_2



$$R = \{(0,0.1), (1,1.2), (1.1,1.2), (2,1.8), (3,3.2)\}$$

$$S_1 \preceq_{0.2} S_2$$

Approximate bisimulation

[Girard & Pappas, TAC-07]

Definition

Consider $S_i = (X_i, X_{0,i}, U_i, \rightarrow_i, Y_i, H_i)$, $i = 1, 2$ with X_1 and X_2 subsets of some set X with metric d and let $\varepsilon \geq 0$ be a given accuracy. A relation

$$R \subseteq X_1 \times X_2$$

is an ε -approximate bisimulation relation between S_1 and S_2 if

1. R is an ε -approximate simulation relation from S_1 to S_2
2. the inverse relation R^{-1} of R , i.e.

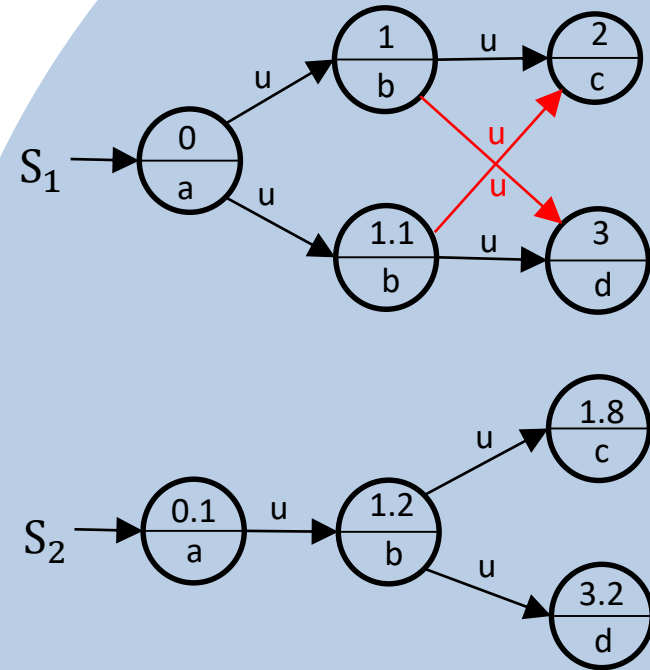
$$R^{-1} = \{(x_2, x_1) \in X_2 \times X_1 \mid (x_1, x_2) \in R\}$$

is an ε -approximate simulation relation from S_2 to S_1

Metric systems S_1 and S_2 are ε -bisimilar, denoted

$$S_1 \simeq_\varepsilon S_2$$

if there exists an ε -approximate bisimulation relation between them



$$R = \{(0, 0.1), (1, 1.2), (1.1, 1.2), (2, 1.8), (3, 3.2)\}$$

$$S_1 \simeq_{0.2} S_2$$

Main result

Theorem

Consider two metric systems $S_i = (X_i, X_{0,i}, U_i, \rightarrow_i, Y_i, H_i)$, $i = 1, 2$ with X_1 and X_2 subsets of some set X with metric d and suppose that $S_1 \preceq_\varepsilon S_2$ for some accuracy $\varepsilon \geq 0$. Consider a set $F_1 \subseteq X_1$ of faulty states for S_1 and define the set

$$F_2 = B_\varepsilon(F_1) \cap X_2$$

of faulty states for system S_2 .

If S_2 is (ρ_2, F_2) -diagnosable for some accuracy $\rho_2 \geq 0$ then, S_1 is (ρ_1, F_1) -diagnosable for all $\rho_1 \geq \rho_2 + 2\varepsilon$.

- This result allows checking approximate diagnosability of a metric system S_1 on the basis of approximate diagnosability of S_2 if $S_1 \preceq_\varepsilon S_2$
- When S_2 has fewer states than S_1 , it can be useful to reduce computational complexity in checking approximate diagnosability of S_1 by using S_2

Main result

- **If one is able to construct a symbolic metric system approximating a continuous or hybrid control system Σ (with an infinite number of states) in the sense of approximate simulation, our result allows checking approximate diagnosability of Σ on the symbolic system**
- Symbolic models approximating continuous or hybrid control systems are extensively studied, see e.g. [Tabuada, Springer-09] and references therein
- Papers working with approximate simulation that fit the framework of this paper are
 - [Pola et al., TAC-16; Pola et al., Autom-08] proposing symbolic models for incrementally stable nonlinear systems
 - [Zamani et al., TAC-12], for possibly unstable nonlinear systems
 - [Girard et al., TAC-10], for incrementally stable switched systems
 - [Pola & Di Benedetto, TAC-14], for piecewise affine systems

We now apply our results to incrementally stable nonlinear systems as studied in [Pola et al., TAC-16]

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Approximate diagnosability of nonlinear systems

Consider the discrete-time nonlinear control system

$$\Sigma: \begin{cases} x(t+1) = f(x(t), u(t)), \\ y(t) = [I_p \quad 0]x(t), \\ x(0) \in \mathbf{X}_0, x(t) \in \mathbb{R}^n, u(t) \in \mathbf{U}, y(t) \in \mathbb{R}^p, t \in \mathbb{N} \end{cases}$$

where:

- $x(t)$ state, $u(t)$ input, $y(t)$ output at time $t \in \mathbb{N}$
- \mathbb{R}^n state space
- $\mathbf{X}_0 \subseteq \mathbb{R}^n$ set of initial states and assumed to be compact
- $\mathbf{U} \subseteq \mathbb{R}^m$ set of inputs, assumed to be compact and containing the origin
- \mathbb{R}^p output space with $p < n$
- $f: \mathbb{R}^n \times \mathbb{R}^m \rightarrow \mathbb{R}^n$ vector field, assumed to be continuous and s.t. $f(0,0) = 0$
- I_p identity matrix in \mathbb{R}^p

Given a set of faulty states $F \subseteq \mathbb{R}^n$ of Σ and a desired accuracy $\rho \geq 0$, how to check (ρ, F) -diagnosability of Σ ?

Approximate diagnosability of nonlinear systems

Metric systems representation of control system Σ :

Given Σ define the metric system

$$S(\Sigma) = (X, X_0, U, \xrightarrow{\quad}, Y, H)$$

where

- $X = \mathbb{R}^n$
- $X_0 = \mathbf{X}_0$
- $U = \mathbf{U}$
- $x \xrightarrow{u} x'$ if $x' = f(x, u)$
- $Y = \mathbb{R}^p$
- $H(x) = [I_p \quad 0]x$ for all $x \in X$

Remarks:

- System $S(\Sigma)$ is metric; we choose metric $\mathbf{d}(x_1, x_2) = \|x_1 - x_2\|$
- System $S(\Sigma)$ is deterministic and **not symbolic**
- System $S(\Sigma)$ preserves many important properties of Σ as for example reachability properties

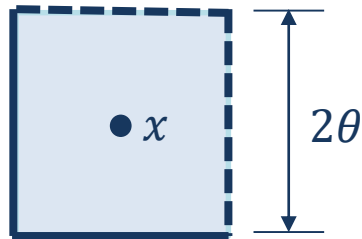
In the sequel we say that Σ is (ρ, F) -diagnosable if $S(\Sigma)$ is so

Approximate diagnosability of nonlinear systems

Discrete abstraction of Σ :

Given $\theta > 0$ and $x = (x_1, x_2, \dots, x_n) \in \mathbb{R}^n$ define the set

$$B_{[-\theta, \theta[}(x) = [x_1 - \theta, x_1 + \theta[\times [x_2 - \theta, x_2 + \theta[\times \dots \times [x_n - \theta, x_n + \theta[$$



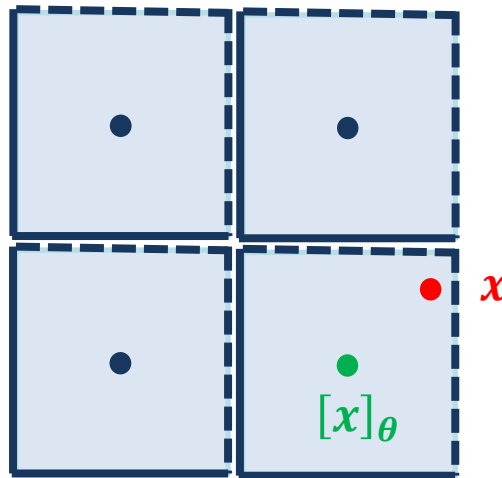
Approximate diagnosability of nonlinear systems

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Given $\theta > 0$ and $x = (x_1, x_2, \dots, x_n) \in \mathbb{R}^n$ define the set

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The collection of sets $B_{[-\theta, \theta[}(x)$ with x ranging in $2\theta\mathbb{Z}^n$ is a partition of \mathbb{R}^n



The (uniform) quantizer in \mathbb{R}^n with accuracy θ is the function

$$[\dots]_{\theta}: \mathbb{R}^n \rightarrow 2\theta\mathbb{Z}^n$$

associating to any $x \in \mathbb{R}^n$ the unique vector $[x]_{\theta} \in 2\theta\mathbb{Z}^n$ such that $x \in B_{[-\theta, \theta[}([x]_{\theta})$

Approximate diagnosability of nonlinear systems

Discrete abstraction of Σ :

Given a state quantization $\eta > 0$ and an input quantization $\mu > 0$ define

$$S_{\eta,\mu}(\Sigma) = (X_{\eta,\mu}, X_{0,\eta,\mu}, U_{\eta,\mu}, \xrightarrow{\eta,\mu}, Y_{\eta,\mu}, H_{\eta,\mu})$$

where

- $X_{\eta,\mu} = [\mathbb{R}^n]_\eta$
- $X_{0,\eta,\mu} = [X_0]_\eta$
- $U_{\eta,\mu} = [U]_\mu$
- $\xi \xrightarrow{v}_{\eta,\mu} \xi'$ if $\xi' = [f(\xi, v)]_\eta$
- $Y_{\tau,\eta} = [\mathbb{R}^p]_\eta$
- $H_{\eta,\mu}(\xi) = [I_p \quad 0]\xi$ for all $\xi \in X_{\eta,\mu}$

Remarks:

- System $S(\Sigma)$ is metric; we choose metric $\mathbf{d}(x_1, x_2) = \|x_1 - x_2\|$
- System $S(\Sigma)$ is **countable** and deterministic

Approximate diagnosability of nonlinear systems

Discrete abstraction of Σ :

We make the following assumption

(A) Control system Σ is incrementally input-to-state stable

Proposition

Under (A), metric system $S_{\eta,\mu}(\Sigma)$ is symbolic

Proposition

Under (A), for any desired accuracy $\varepsilon > 0$ there exists a choice of the quantization parameters $\eta, \mu > 0$ such that $S(\Sigma)$ and $S_{\eta,\mu}(\Sigma)$ are ε -bisimilar

We now use $S_{\eta,\mu}(\Sigma)$ to study approximate diagnosability of Σ

Approximate diagnosability of nonlinear systems

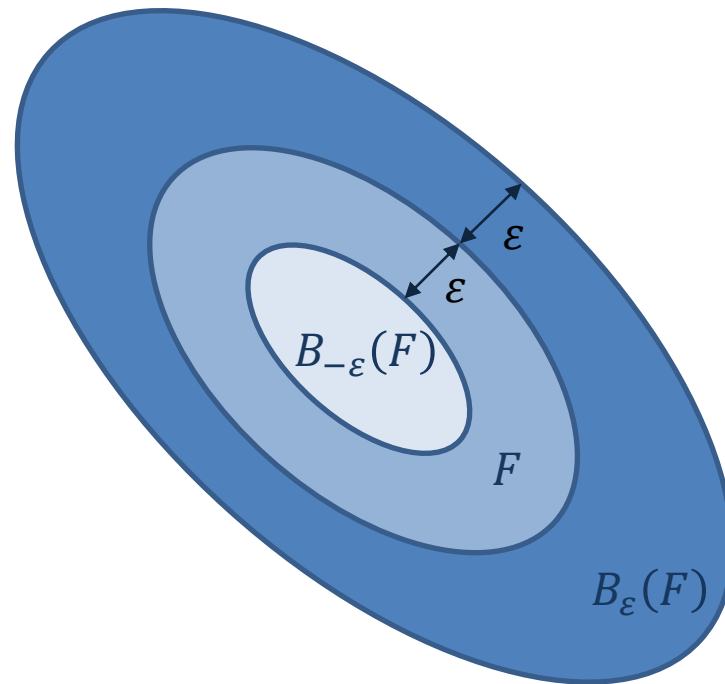
Corollary

Consider a set $F \subseteq X$ of faulty states of Σ with $F \cap X_0 = \emptyset$ and define

$$F_\varepsilon = B_\varepsilon(F) \cap [\mathbb{R}^n]_\eta$$

$$F'_\varepsilon = B_{-\varepsilon}(F) \cap [\mathbb{R}^n]_\eta$$

$$B_{-\varepsilon}(F) = \{x \in F \mid B_\varepsilon(x) \subseteq F\}$$



Approximate diagnosability of nonlinear systems

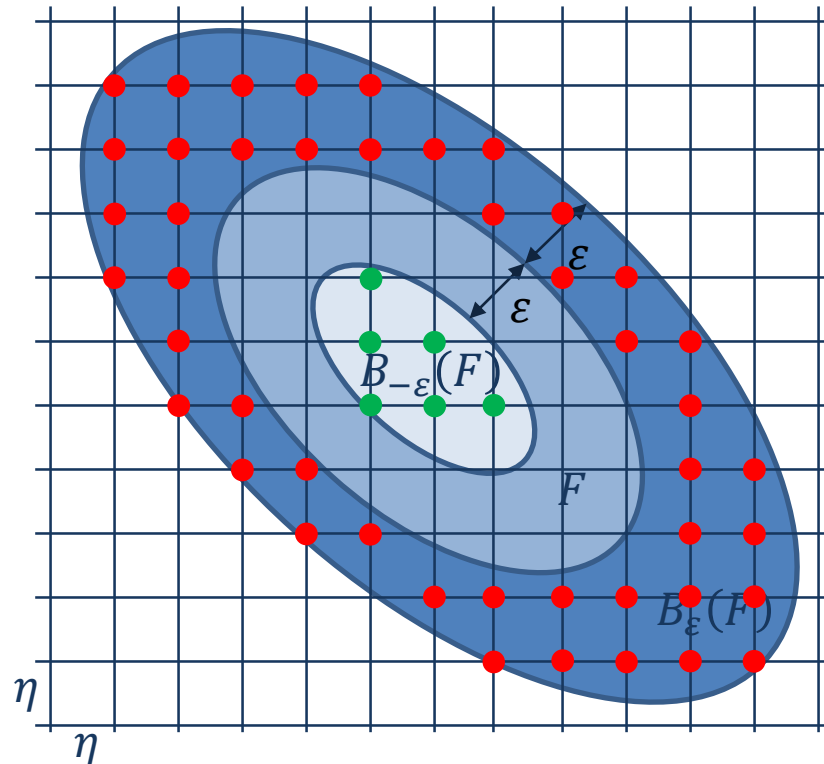
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Approximate diagnosability of nonlinear systems

Corollary

Consider a set $F \subseteq X$ of faulty states of Σ with $F \cap X_0 = \emptyset$ and define

$$F_\varepsilon = B_\varepsilon(F) \cap [\mathbb{R}^n]_\eta$$

$$F'_\varepsilon = B_{-\varepsilon}(F) \cap [\mathbb{R}^n]_\eta$$

$$B_{-\varepsilon}(F) = \{x \in F \mid B_\varepsilon(x) \subseteq F\}$$

Suppose that assumption (A) holds and for any desired accuracy $\varepsilon > 0$ pick quantization parameters $\eta, \mu > 0$ such that $S(\Sigma)$ and $S_{\eta,\mu}(\Sigma)$ are ε -bisimilar. Then:

- If $S_{\eta,\mu}(\Sigma)$ is $(k\eta, F_\varepsilon)$ -diagnosable for some $k \in \mathbb{N}$ then Σ is (ρ, F) -diagnosable, for any $\rho > 2\varepsilon + k\eta$
- Suppose that F is with interior and $\varepsilon > 0$ is such that $F'_\varepsilon \neq \emptyset$. If Σ is (ρ, F) -diagnosable for some $\rho \geq 0$, then $S_{\eta,\mu}(\Sigma)$ is $(k'\eta, F'_\varepsilon)$ -diagnosable, for any $k' > \min\{h \in \mathbb{N} \mid \rho + 2\varepsilon \leq h\eta\}$

Remark

First statement can be used to check if Σ is approximately diagnosable while second statement (in its logical negation form) to check if Σ is not approximately diagnosable

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Example

Consider the following nonlinear control system:

$$\Sigma: \begin{cases} x_1(t+1) = 0.15(\cos(x_1(t) - 1)) + 0.18(\operatorname{sech}(x_2(t) - 1)) + u \\ x_2(t+1) = 0.22 \sin(x_2(t)) + 0.25 \tanh(x_1(t)) \\ y(t) = x_1(t) \end{cases}$$

with $x(0) = (x_1(0), x_2(0)) \in \mathbf{X}_0$, $u(t) \in \mathbf{U} = [-2.5, 2.5]$

- It is possible to show that Σ is incrementally input-to-state stable
- For a desired accuracy $\varepsilon = 1$ by picking $\eta = 0.045$ and $\mu = 0.01$ we get that $S(\Sigma)$ and $S_{\eta, \mu}(\Sigma)$ are ε -bisimilar

Example

We consider two cases:

- For $X_0 = [-1.25, 1.25] \times [6.75, 8.55]$ and $F = [-2.8, 2.6] \times [-0.1, 0.1]$ we get that Σ is **(ρ, F) -diagnosable, for any $\rho > 2.09$**

Details:

- $S_{\eta, \mu}(\Sigma)$ is $(2\eta, F_\varepsilon)$ -diagnosable
 - $S_{\eta, \mu}(\Sigma)$ is with 1,145 (accessible) states and 64,782 transitions
 - time of computation for constructing $S_{\eta, \mu}(\Sigma) = 10.313$ min
 - time of computation for checking $(2\eta, F_\varepsilon)$ -diagnosability of $S_{\eta, \mu}(\Sigma) = 4.0127$ h
- For $X_0 = [6.75, 8.55] \times [-1.25, 1.25]$ and $F = [-1.1, 1.1] \times [-1.1, 1.1]$ we get that Σ is **not (ρ, F) -diagnosable, for any $\rho < 0.07$**

Details:

- $S_{\eta, \mu}(\Sigma)$ is not $(46\eta, F'_\varepsilon)$ -diagnosable
- $S_{\eta, \mu}(\Sigma)$ is with 1,141 (accessible) states and 64,662 transitions
- time of computation for constructing $S_{\eta, \mu}(\Sigma) = 10.972$ min
- time of computation for checking $(46\eta, F'_\varepsilon)$ -diagnosability of $S_{\eta, \mu}(\Sigma) = 2.315$ h

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References

- **[De Persis, CDC-13]** C. De Persis. Detecting faults from encoded information. IEEE Conference on Decision and Control, 2013
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Conclusions

In this paper

- General class of metric systems
- Novel notion of approximate diagnosability
- Relations between approximate diagnosability and approximate simulations
- Application to approximate diagnosability of nonlinear control systems

Further work

Efficient algorithms for checking approximate diagnosability of nonlinear control systems

... thanks!

On Approximate Diagnosability of Metric Systems

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